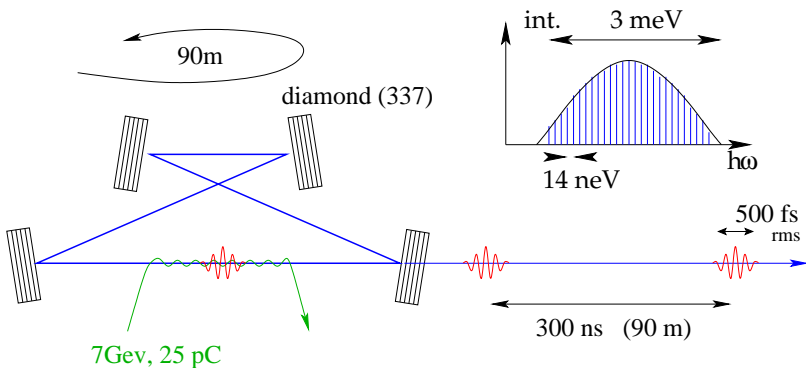


# XFEL

Design example: XFEL for 14.4 keV

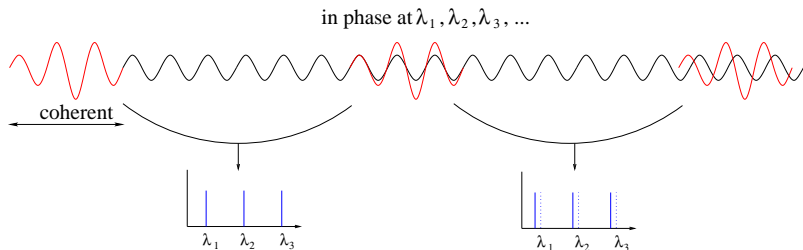


Kwang-Je Kim et al.: PRL **100**, 244802 (2008)  
PRST-AB **12**, 030703 (2009)

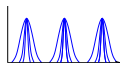
$6.5 \cdot 10^8$  photons/pulse

parameters from R. Lindberg (ANL)

**XFELO** XFELO has full longitudinal coherence within each pulse but no pulse-to-pulse coherence without cavity-length stabilization of course one pulse is always coherent with the next at suitable  $\lambda_i$  but different  $\lambda_i$  for next pulse pair ..



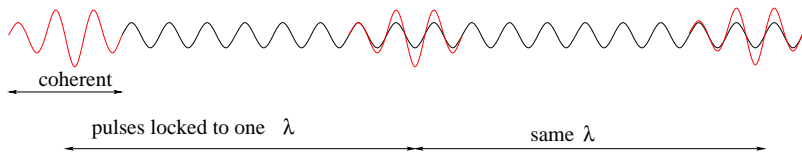
lines broaden as cavity length jitters  
uniformly distributed for  $t \rightarrow \infty$



$\rightarrow$  no coherence in the ensemble / ergodic average

## XFELO

need an external reference to determine  $\lambda$   
so that pulses are phased to each other at this  $\lambda$

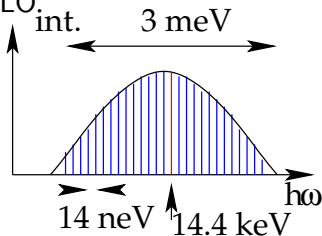


How can we do that? – use nuclear resonance as external reference  
With this, the XFELO can duplicate the coherence properties of  
optical lasers used in metrology

## XFELO

example  $^{57}\text{Fe}$  with 5 neV natural linewidth,  
 (or 8 neV after some inhomogeneous broadening ( $\text{FeK}(\text{CN})_6$ ))  
 can resolve 14 neV mode spacing of XFELO.

stabilize the cavity to make  
*one* mode resonant with  $^{57}\text{Fe}$   
 → stable frequency comb



→ intense coherent radiation for metrology, fundamental physics

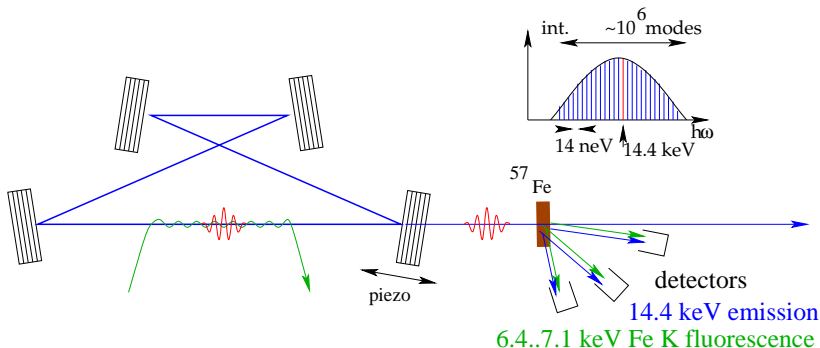
noise sources to address:

gain-related: spontaneous emission, gain fluctuation

cavity-length fluctuations: seismic, heat load fluctuations

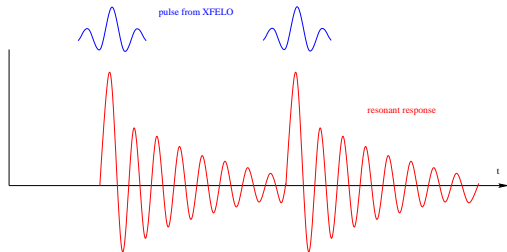
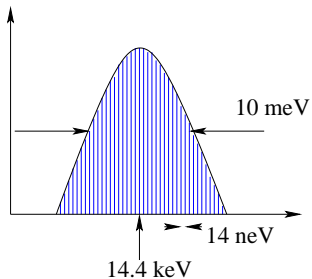
## Cavity Stabilization - I

measure resonance of  $^{57}\text{Fe}$  sample, adjust cavity length with piezo:



## Cavity Stabilization - I

frequency vs. time domain



longitudinal modes spaced at  
cavity round-trip frequency  
one in resonance with  $^{57}\text{Fe}$

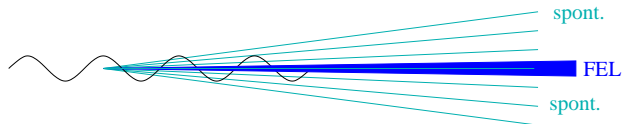
phase relation of wavepackets  
relative to previously excited  
free oscillation of nuclear dipoles

## Sources of Phase Noise

- 1) spontaneous emission into lasing mode:  
 $10^{-8}$  in intensity,  $10^{-4}$  in amplitude

electron bunches

(classical spontaneous undulator radiation)



linewidth from spont. emission:

$$10^{-12} \text{ eV}$$

BWA &amp; KJK, PRST-AB 18, 030711 (2015)

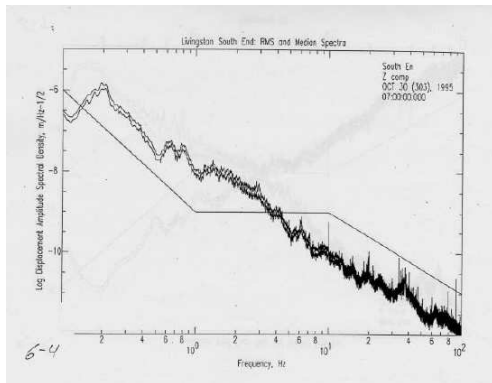
noise in modulus is limited  
 by loss/gain balance  
 only phase noise remains

- 2) fluctuations in electron bunches:

gain fluctuations due to bunch charge and electron energy  
 bunch arrival time fluctuations broaden comb lines  
 effect estimated at  $10^{-3}$  level

## Sources of Phase Noise

ground motion (seismic)



<http://www.ligo.caltech.edu/docs/G/G010325-00.pdf>

ground motion, cavity mirrors

ground motion

amplitude  $A(f)$

$$10^{-9} \frac{m}{\sqrt{Hz}} \left( \frac{10\text{Hz}}{f} \right)^2$$

so,

$$\sqrt{\int_{f_0}^{1/T} df \frac{A^2(f)}{Tf}} < \frac{\lambda}{100}$$

for  $f_0 > 8\text{kHz}$

30-kHz feedback loop  
can handle this

and better with mechanical damping

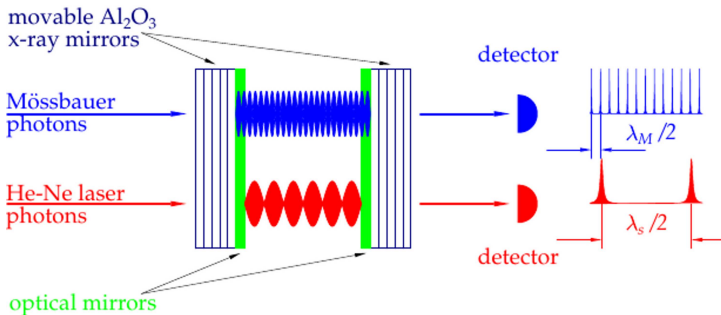


## Applications: Length/Time Standard

Use NR as length standard: Shvyd'ko et al., PRL **85**, 495 (2000)

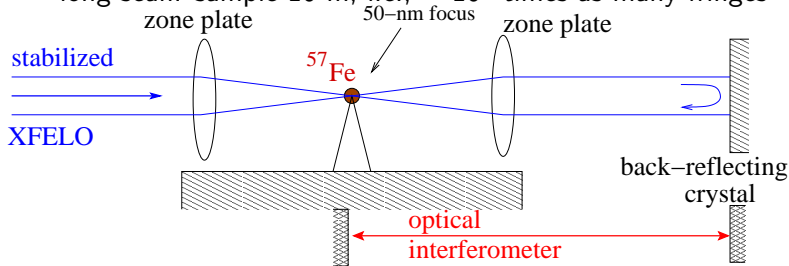
combined x-ray / optical Fabry-Perot interferometer (FPI)

Yu. V. Shvyd'ko, 2004



## Applications: Length/Time Standard

improvement:

long scan: sample 10 m, i.e.,  $\sim 10^4$  times as many fringes

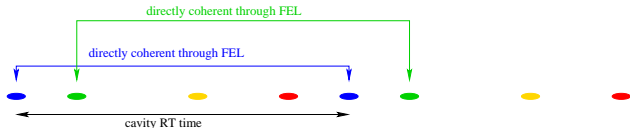
Traveling assembly: focusing/collimating zone plates and  
a **single**  $^{57}\text{Fe}$  atom embedded in a crystal

With 50-nm focus, abs.  $\sigma = 10^{-22}\text{m}^2$ , 1000 resonant photons / pulse  
about 100 absorption events / sec.

Sparse sampling, using known  $\lambda$  to 7 places

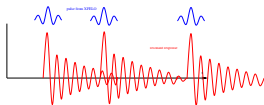
## Weird Tricks on the Comb

inject bunches at a rate that is a harmonic or a sub-harmonic of the cavity round-trip time



first, get sub-populations of pulses related by cavity RT time

Then, the external NR reference will enforce coherence among them



strong NR response only if  
sub-populations are in phase

can do Fibonacci sequences of bunch intervals, etc.