

New Techniques and Methods

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DESY

New Techniques and Methods

Explore the opportunities for different x-ray analytical techniques:

- high brilliance:
many photons in small phase space volume
- diffraction limit:
spatial coherence: all photons prepared in same initial state
(for given color)
in practice: coherence length exceeds lateral beam size

Obvious advantages for high-brilliance applications:

- improved photon statistics:
low background
large signal in short time
- ➔ high sensitivity, high spatial and temporal resolution

New Techniques and Methods

Explore the opportunities for different x-ray analytical techniques:

- correlation spectroscopies: XPCS
- scanning probes (diffraction limited nanoprobes)
- coherent x-ray diffraction techniques (CXDI, ptychography, ...)
- macromolecular crystallography (MX)
- ...




New Techniques and Methods

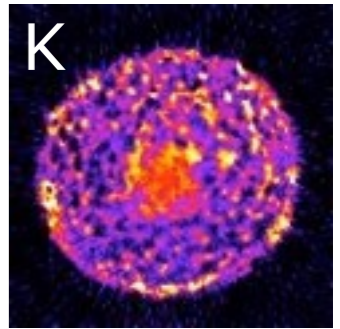
Challenges:

- beamline: stability
- beamline: background radiation
- sample: radiation damage
- ...

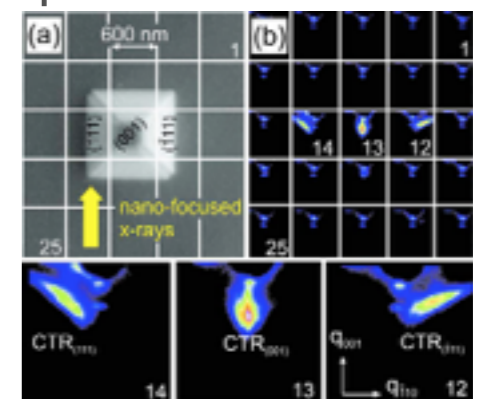
X-Ray Microscopy on the Nanometer Scale

Broad field of applications:

-  Physics, chemistry, biology, earth- and environmental science, nano-technology, ...
-  Main advantage: large penetration depth
 - in-situ and in-operando studies
-  X-ray analytical contrasts: XRD, XAS, XRF, ...
 - atomic scale resolution

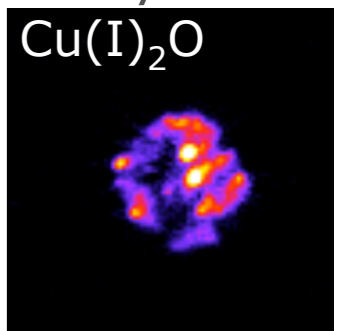


quantum dots






M. Hanke, et al.,
APL **92**, 193109 (2008)

catalysts



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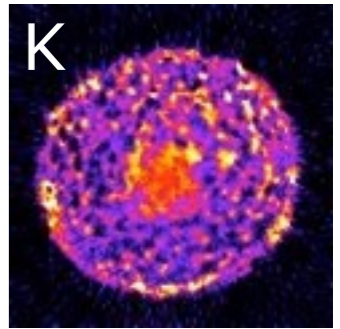
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Today: "Mesoscopic gap"

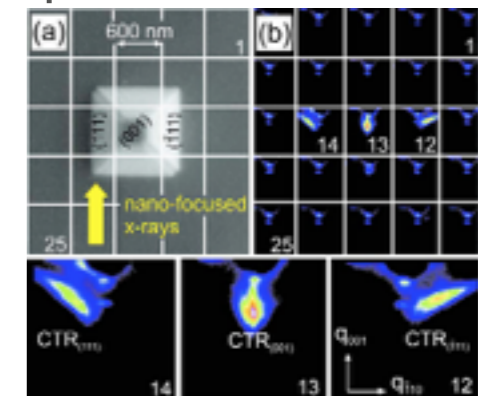
real-space resolution: down to about 10 nm

XRD and XAS: atomic scale

What happens on (mesoscopic) 1 - 10 nm scale?

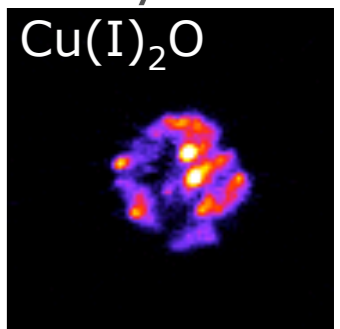


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X-Ray Microscopy on the Nanometer Scale

Today: "Mesoscopic gap"

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XRD and XAS: atomic scale

What happens on (mesoscopic) 1 - 10 nm scale?

Many interesting physics and chemistry questions:

investigate local states:

- individual defects (0D): changes in electron density, charge ordering
- (structural) domain boundaries (2D), e. g., in multiferroics
- mesoscopic dynamics at (solid-state) phase transitions
- catalytic nanoparticles (activity in operando)
- ...

Mesoscale also very important for nanotechnology (e. g., defects in devices)!

Current State in X-Ray Microscopy

Conventional x-ray microscopy

→ optics limit spatial resolution: diffraction limited focusing

$$d_t \approx \frac{\lambda}{2NA} \quad (\text{typically: a few tens of nanometers})$$

optics are technology limited!

Theoretical extrapolation of x-ray optical performance to the atomic level.

[PRB **74**, 033405 (2006); H. Yan, et al., PRB **76**, 115438 (2007)]

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Coherent x-ray imaging techniques (CXDI, ptychography)

→ no imaging optic!

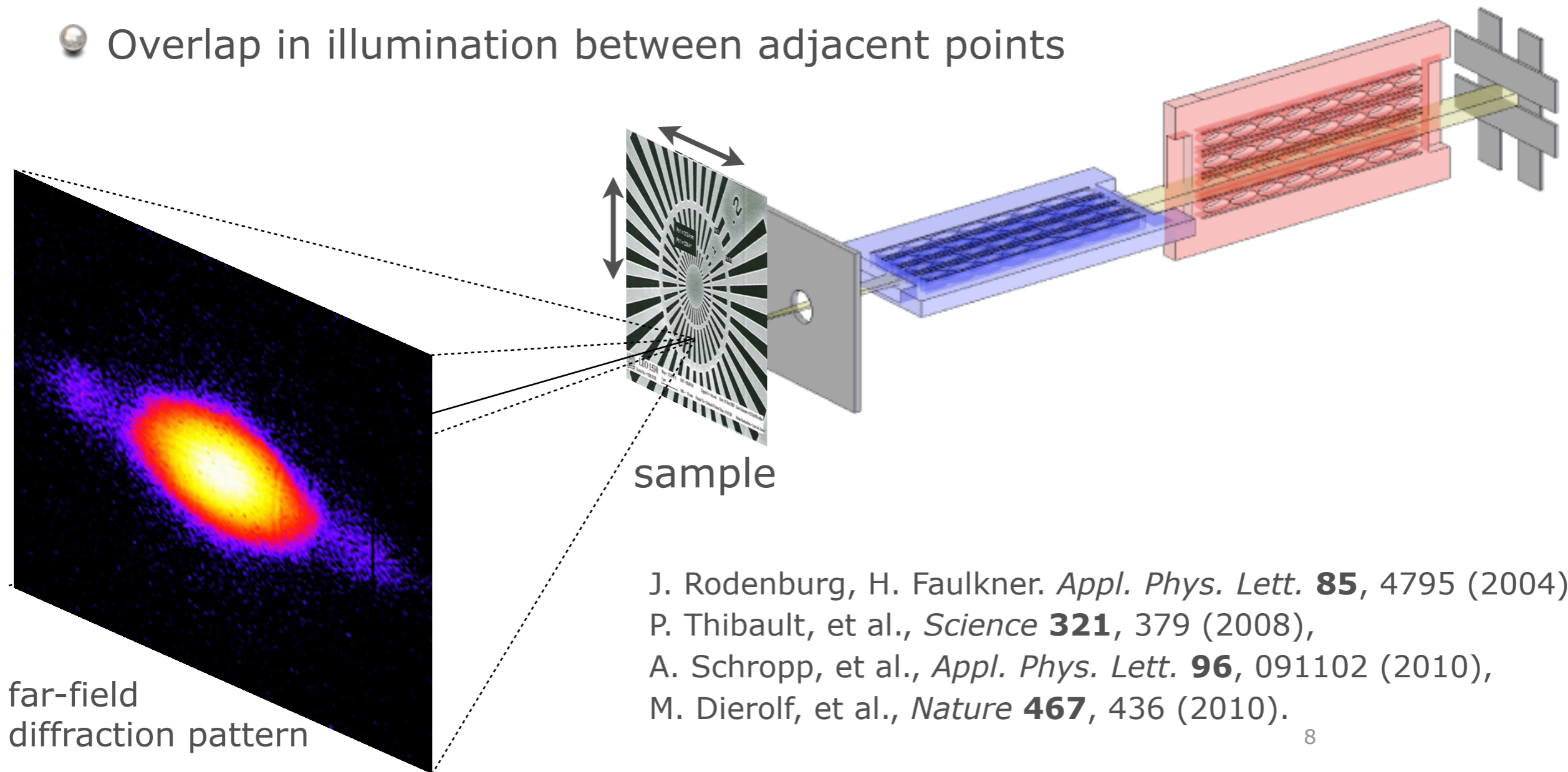
→ limited by statistics of far-field diffraction patterns ...

highest resolution: a few nanometers, focusing coherent beam

[PRL **101**, 090801 (2008); Y. Takahashi, et al., PRB **80**, 054103 (2009);
A. Schropp, et al., APL **100**, 253112 (2012)]

Scanning Coherent X-Ray Diffraction Imaging: Ptychography

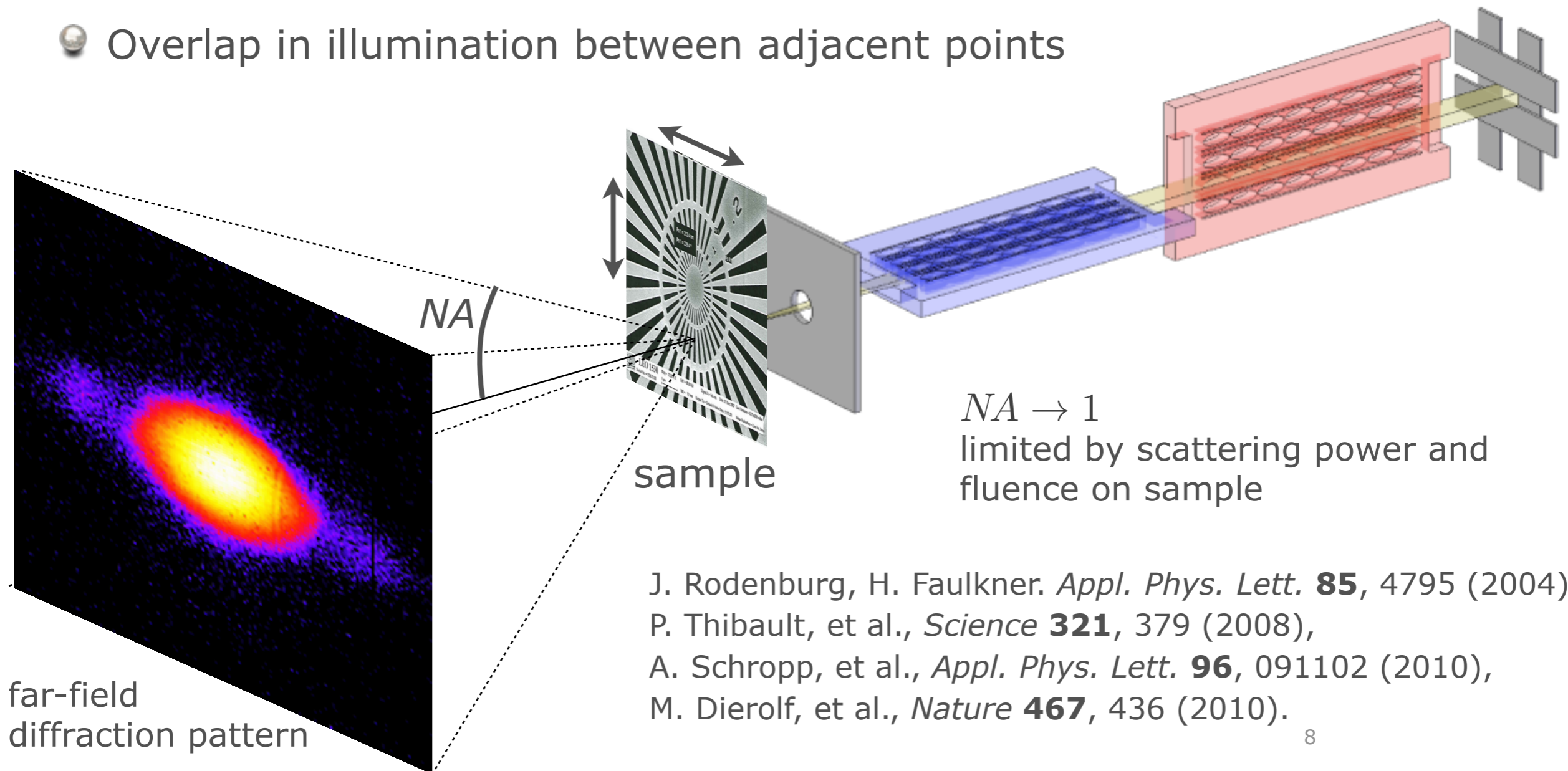
- Sample is raster scanned through confined beam
- At each position of scan: diffraction pattern is recorded
- Overlap in illumination between adjacent points



J. Rodenburg, H. Faulkner. *Appl. Phys. Lett.* **85**, 4795 (2004),
P. Thibault, et al., *Science* **321**, 379 (2008),
A. Schropp, et al., *Appl. Phys. Lett.* **96**, 091102 (2010),
M. Dierolf, et al., *Nature* **467**, 436 (2010).

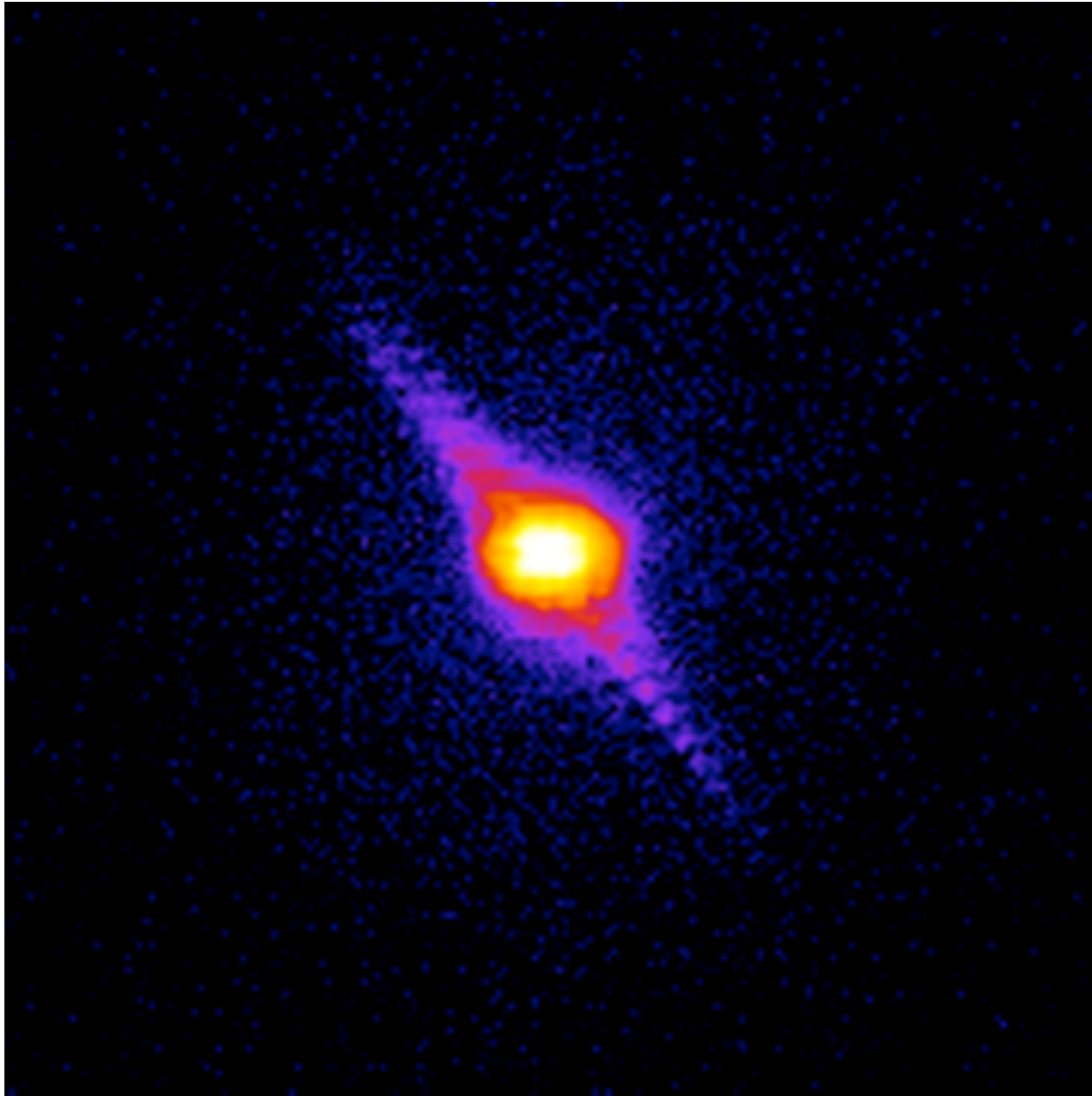
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Ptychographic Microscopy



Experiment at P06:

detector:

Pilatus 300k (172 μ m pixel size)

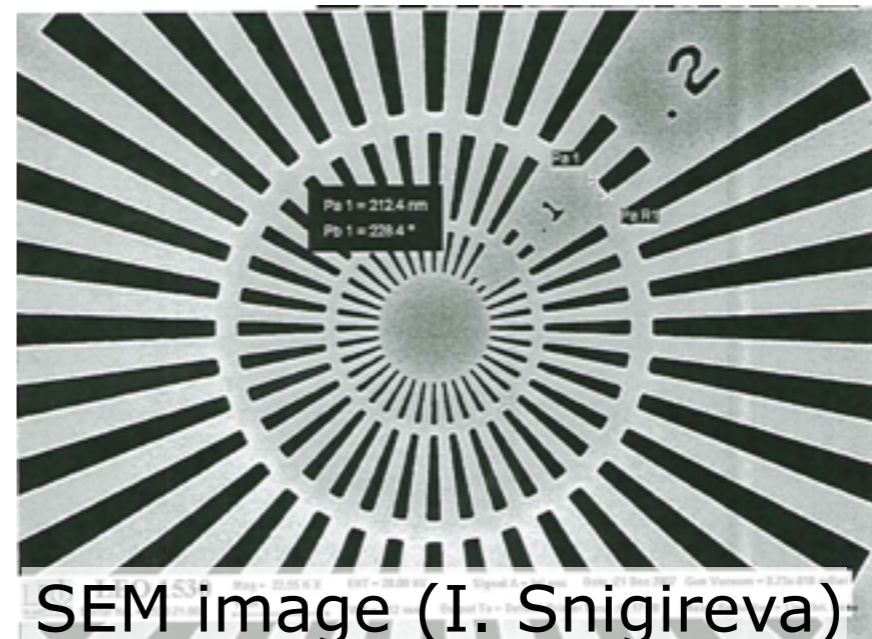
sample-detector distance:

2080 mm

exposure time:

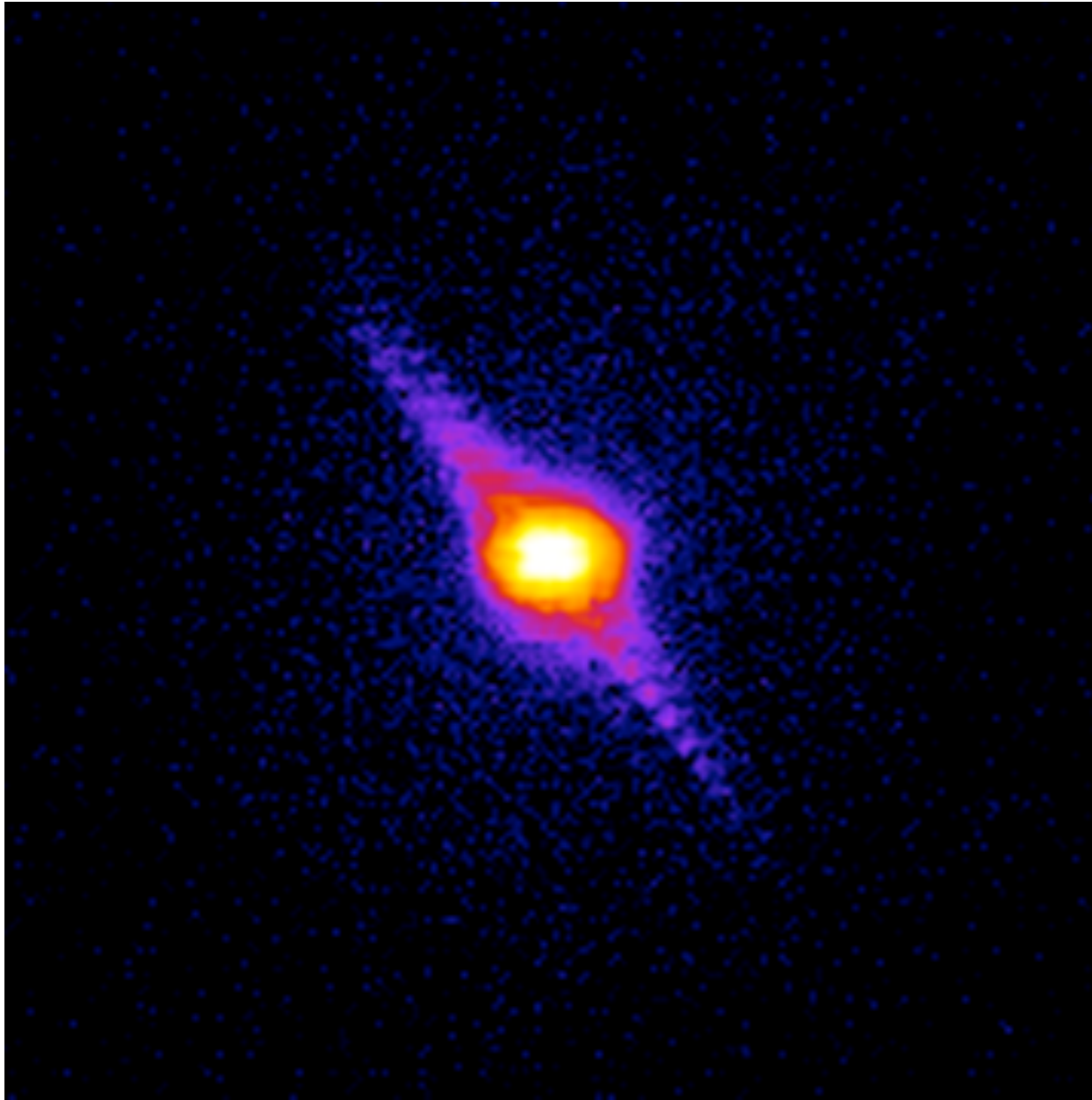
1.5 s per point

Sample: NTT AT test pattern



SEM image (I. Snigireva)

Ptychographic Microscopy



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Pilatus 300k (172 μ m pixel size)

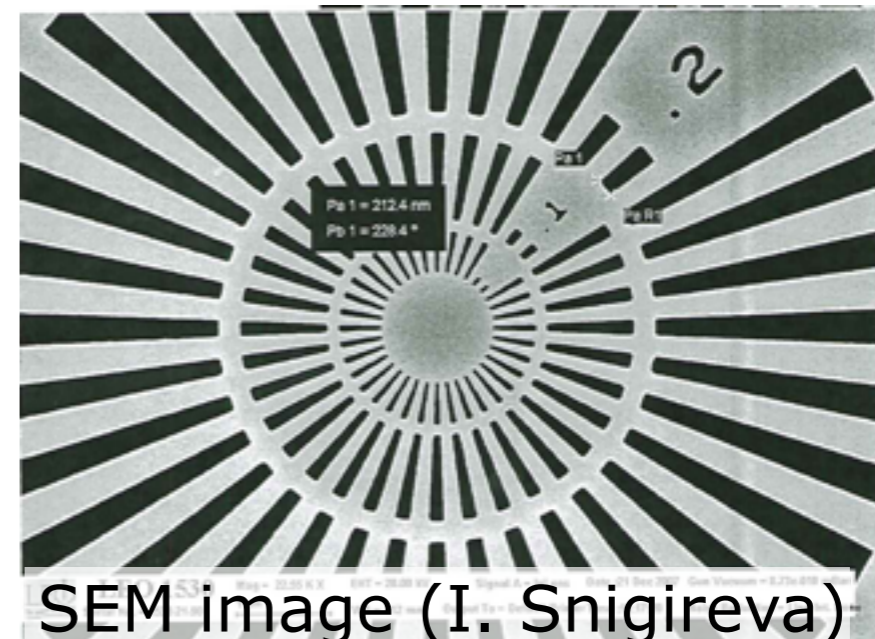
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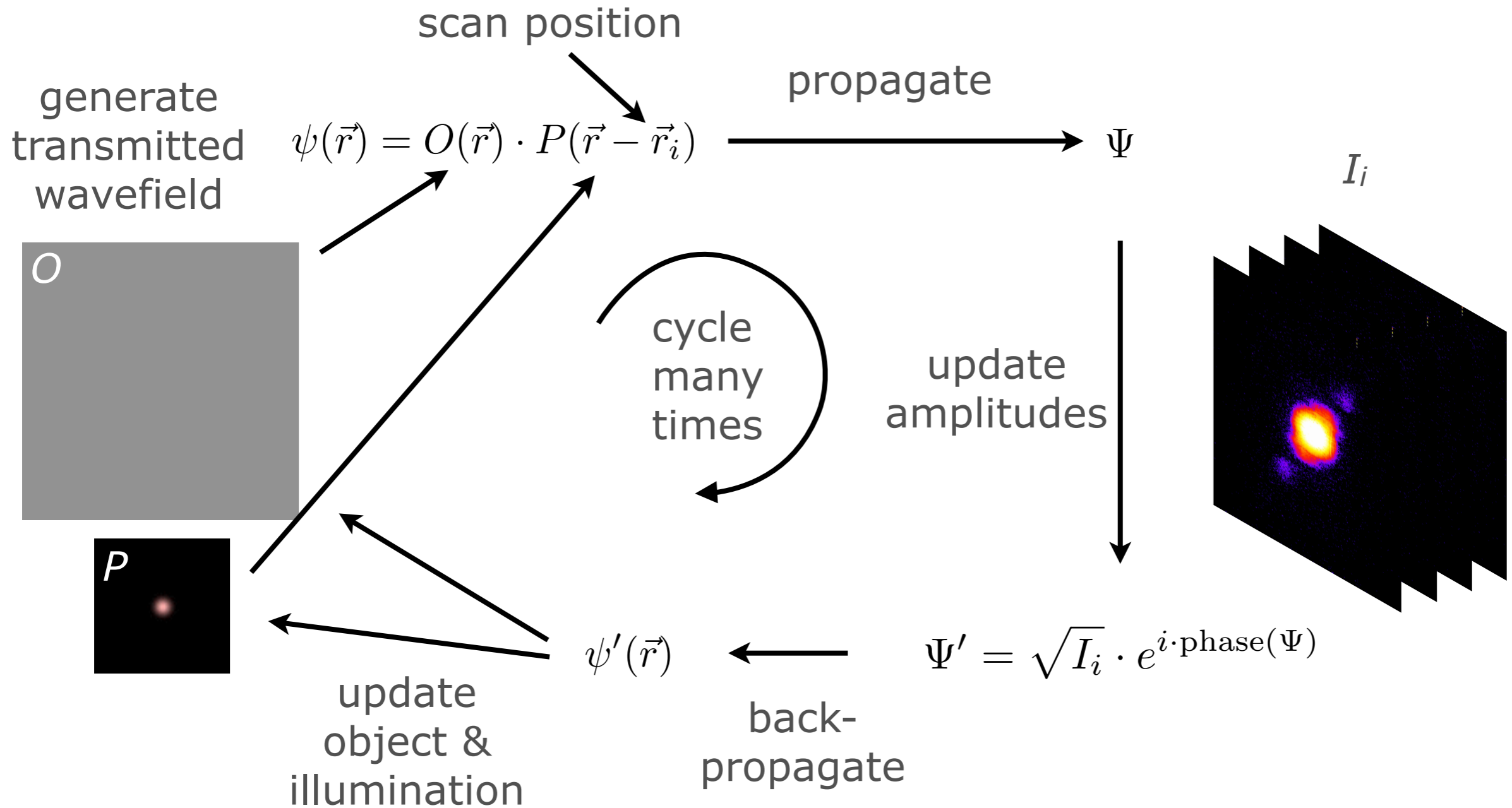
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Sample: NTT AT test pattern



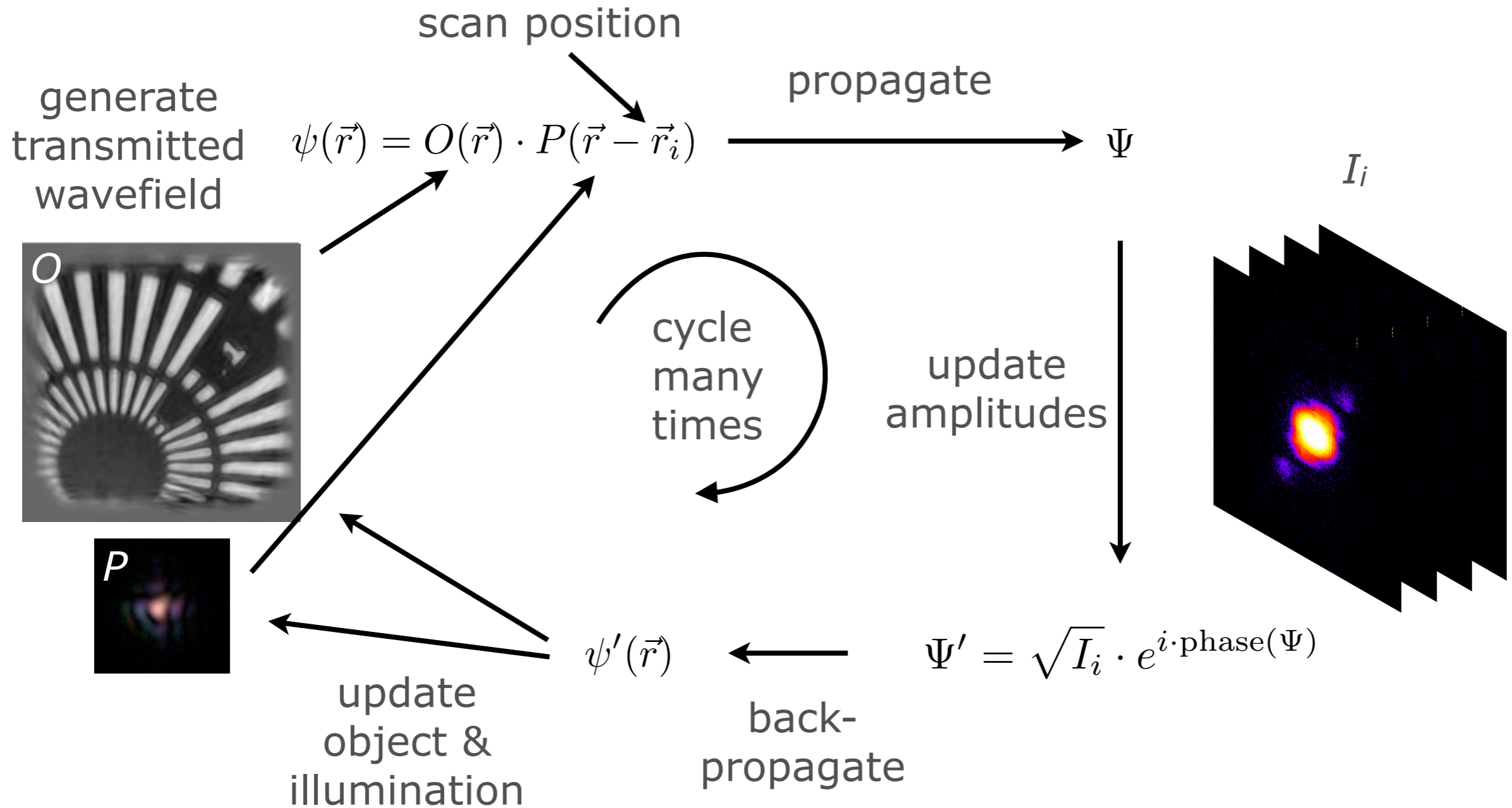
SEM image (I. Snigireva)

Ptychography: Reconstruction



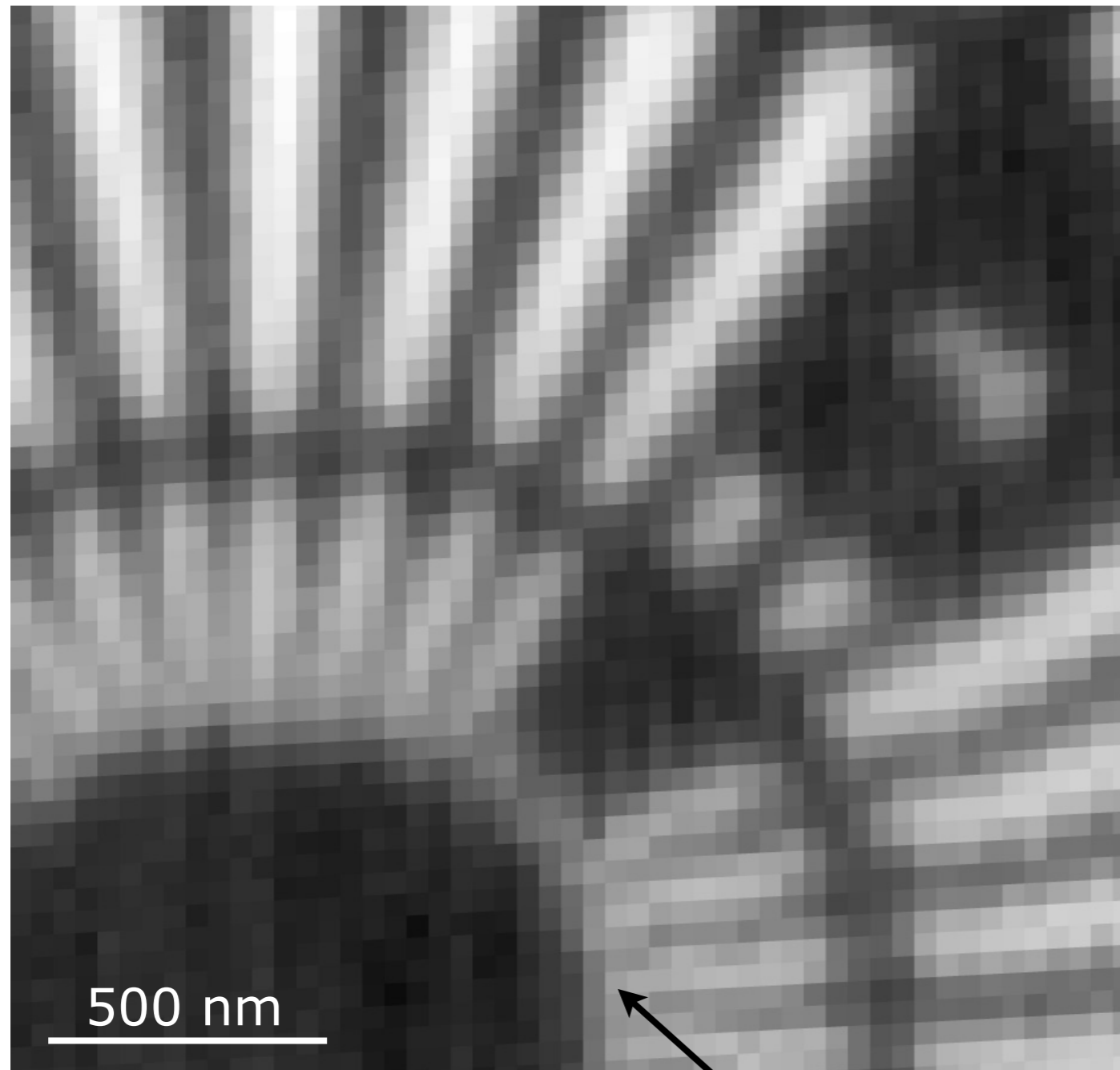
Maiden & Rodenburg, Ultramicroscopy **109**, 1256 (2009).

Ptychography: Reconstruction



Maiden & Rodenburg, Ultramicroscopy **109**, 1256 (2009).

Scanning Microscopy: Fluorescence Imaging



Ta L α fluorescence

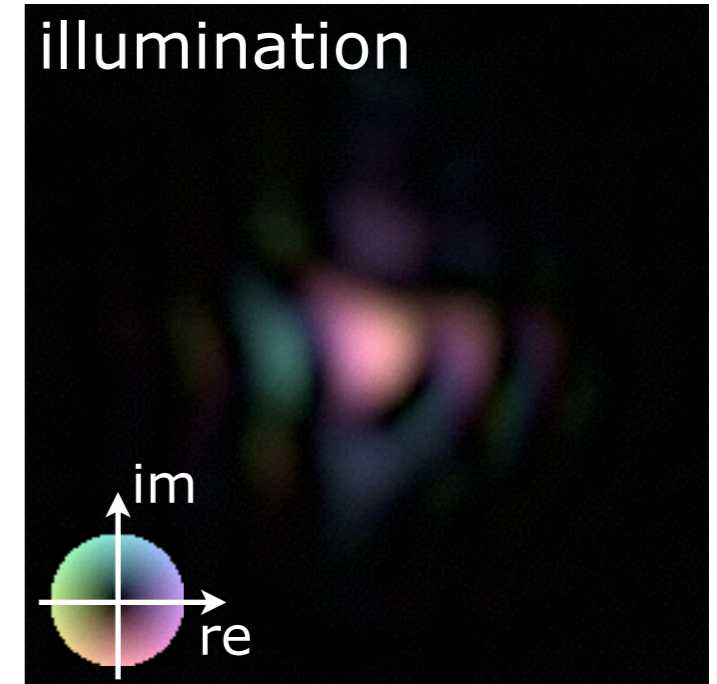
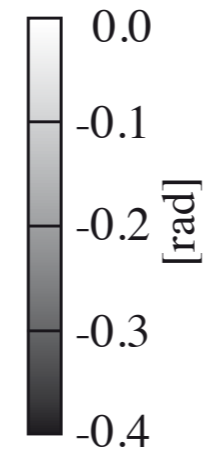
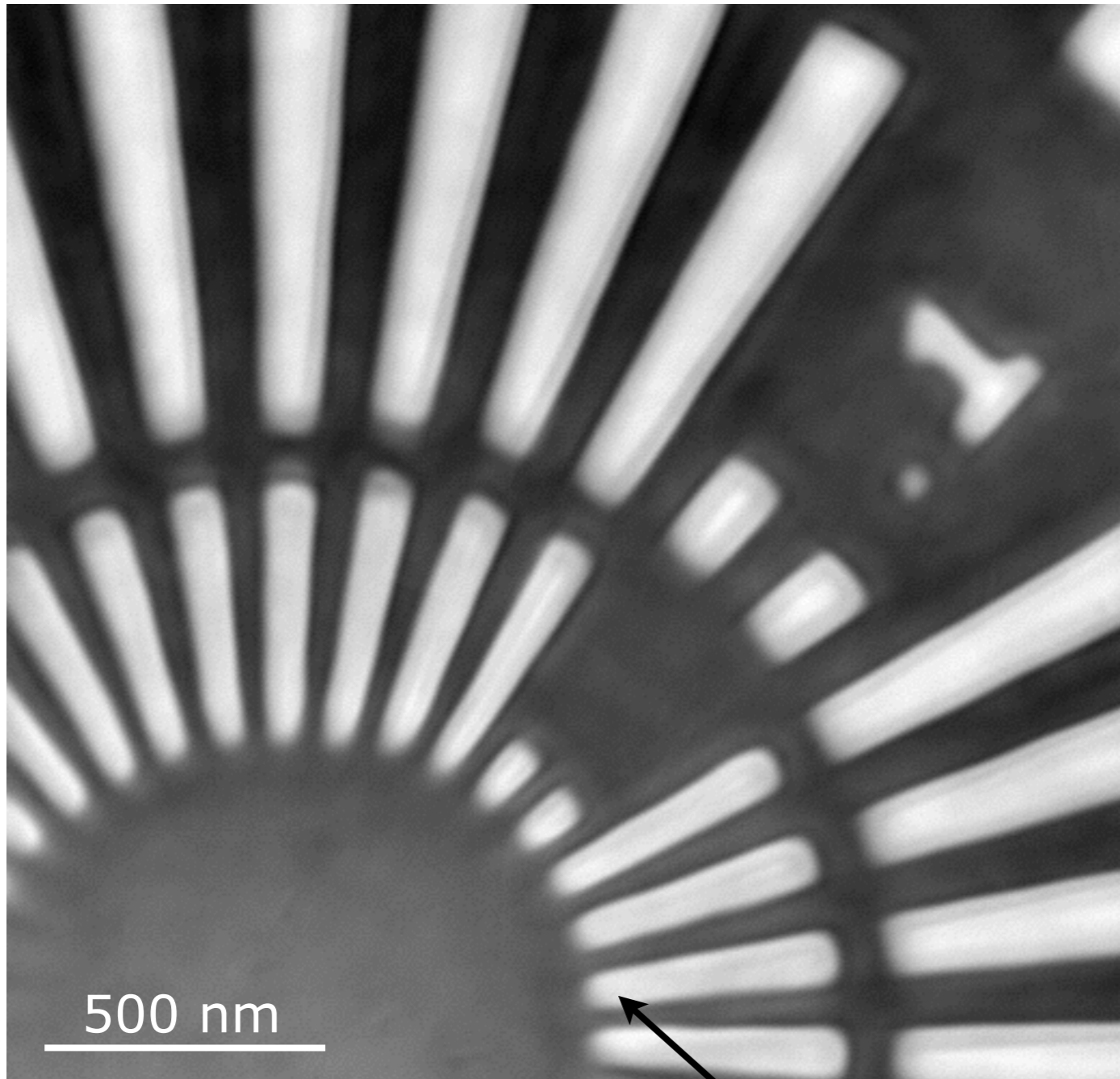
$E = 15.25$ keV

50 x 50 steps of 40 x 40 nm²

2 x 2 μ m² FOV

exposure: 1.5 s per point

Scanning Microscopy: Ptychography

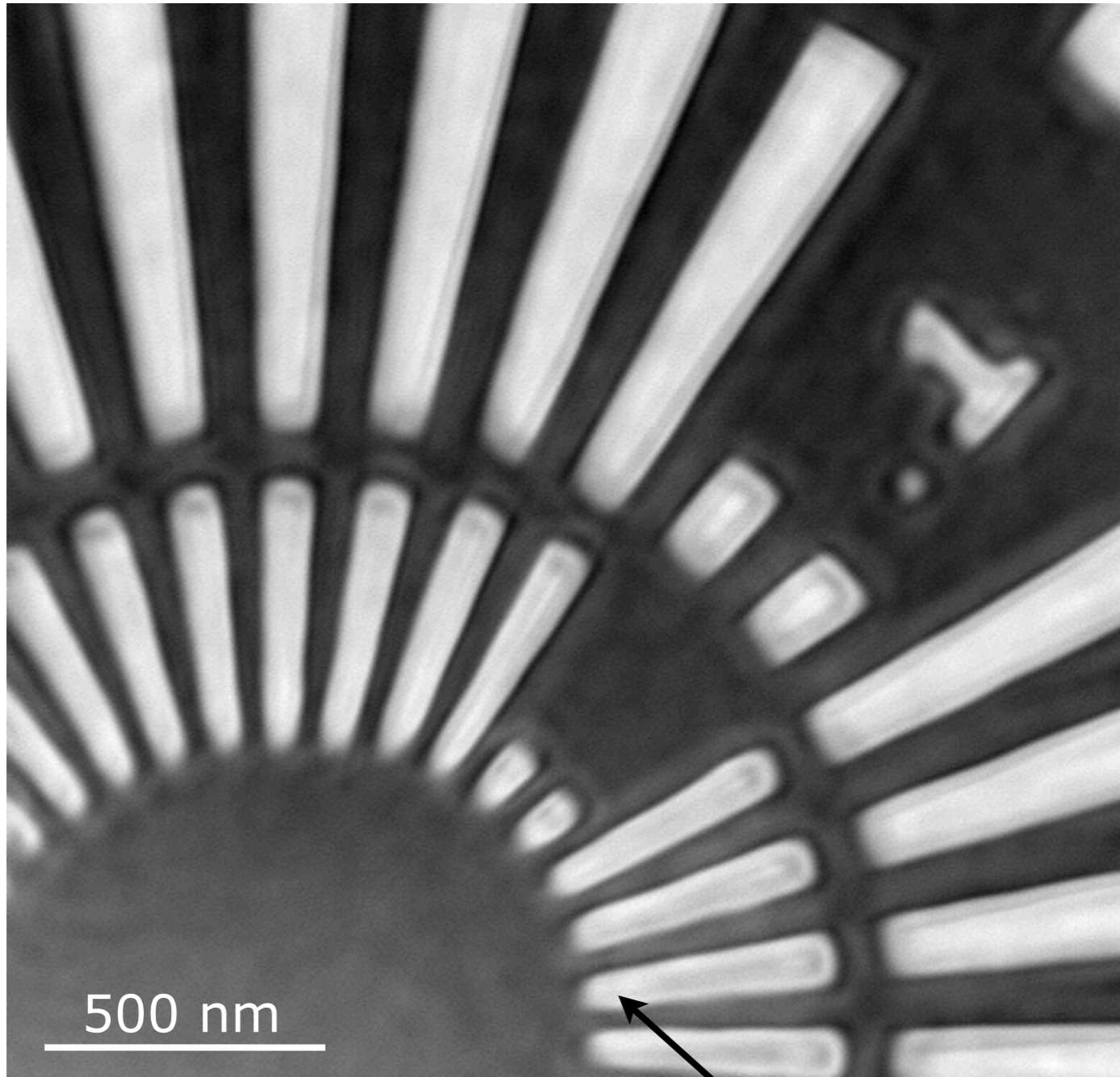


A. Schropp, et al., APL **96**, 091102 (2010),
S. Hönig, et al., Opt. Exp. **19**, 16325 (2011).

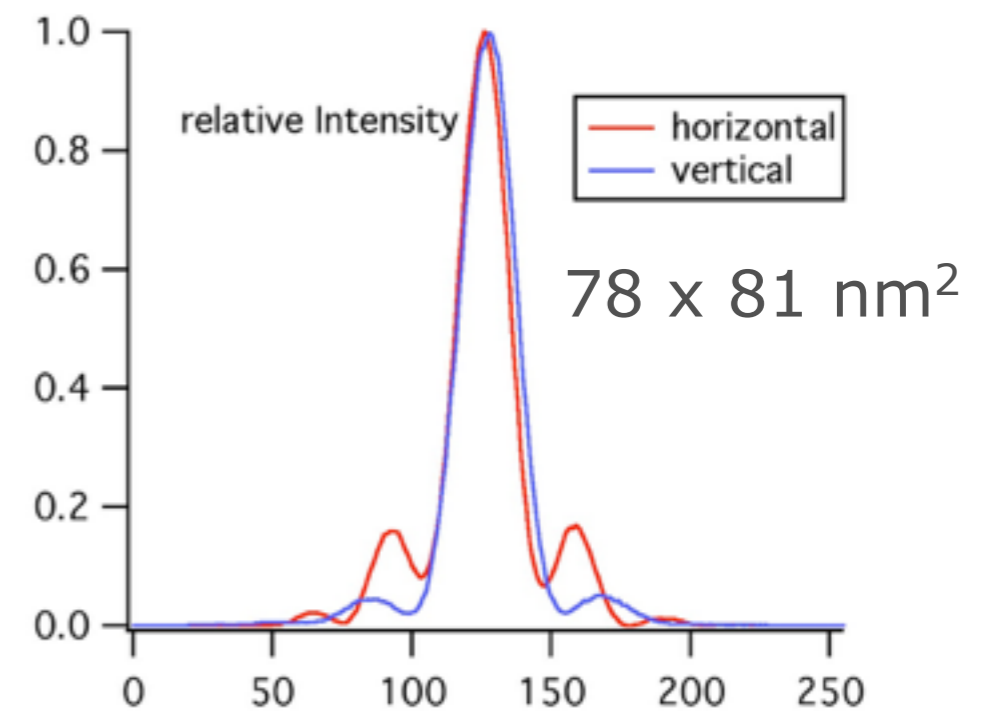
$E = 15.25$ keV
 50 x 50 steps of 40×40 nm²
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 exposure: 1.5 s per point
 detected fluence: $2.75 \cdot 10^4$ ph/nm²

A. Schropp, et al., APL **100**, 253112 (2012).

Scanning Microscopy: Ptychography



illumination



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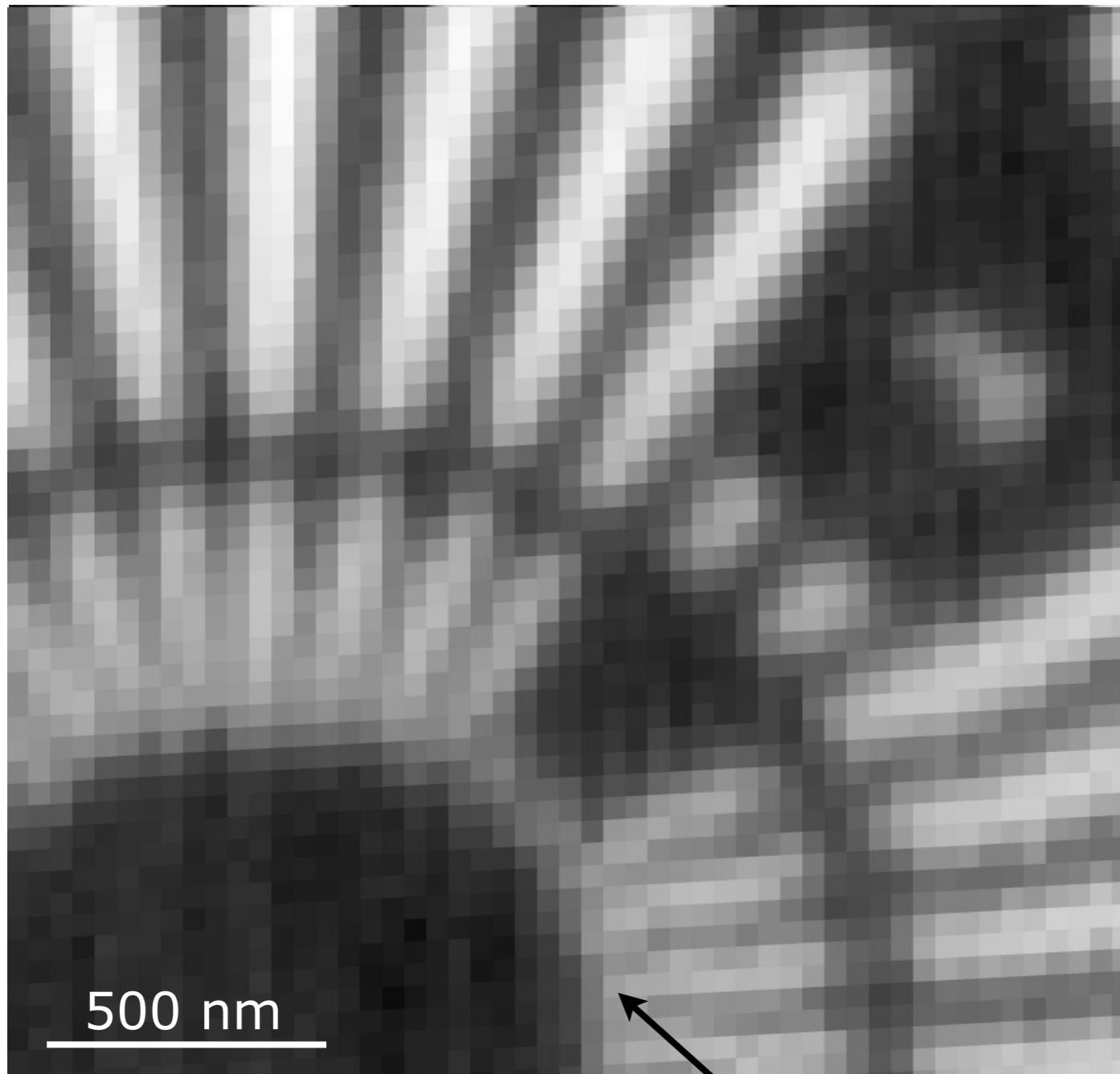
2 x 2 μm² FOV

exposure: 1.5 s per point

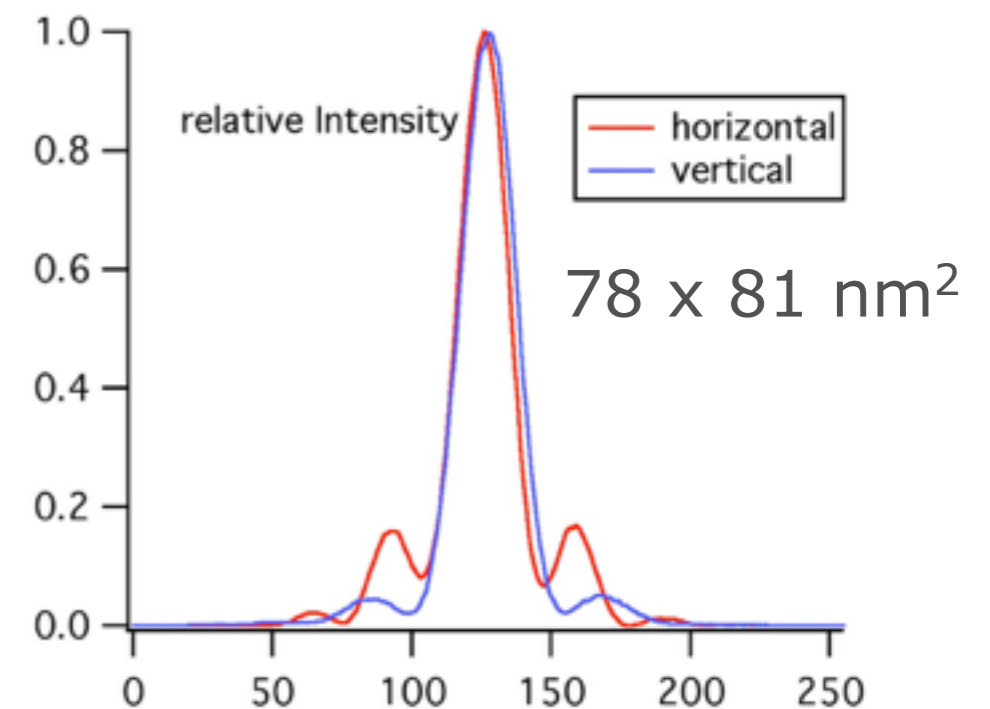
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Scanning Microscopy: Ptychography



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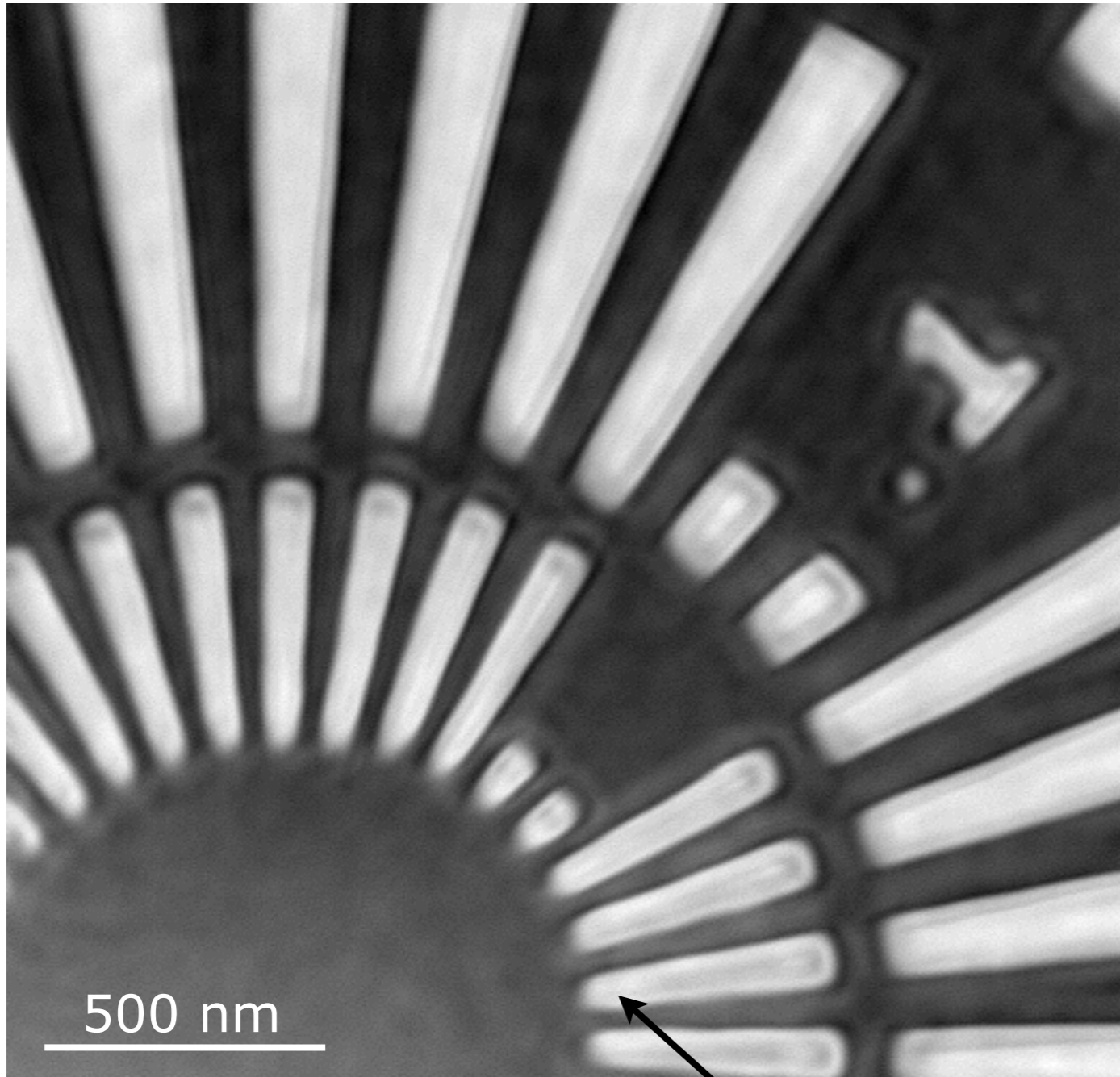
2 x 2 μm^2 FOV

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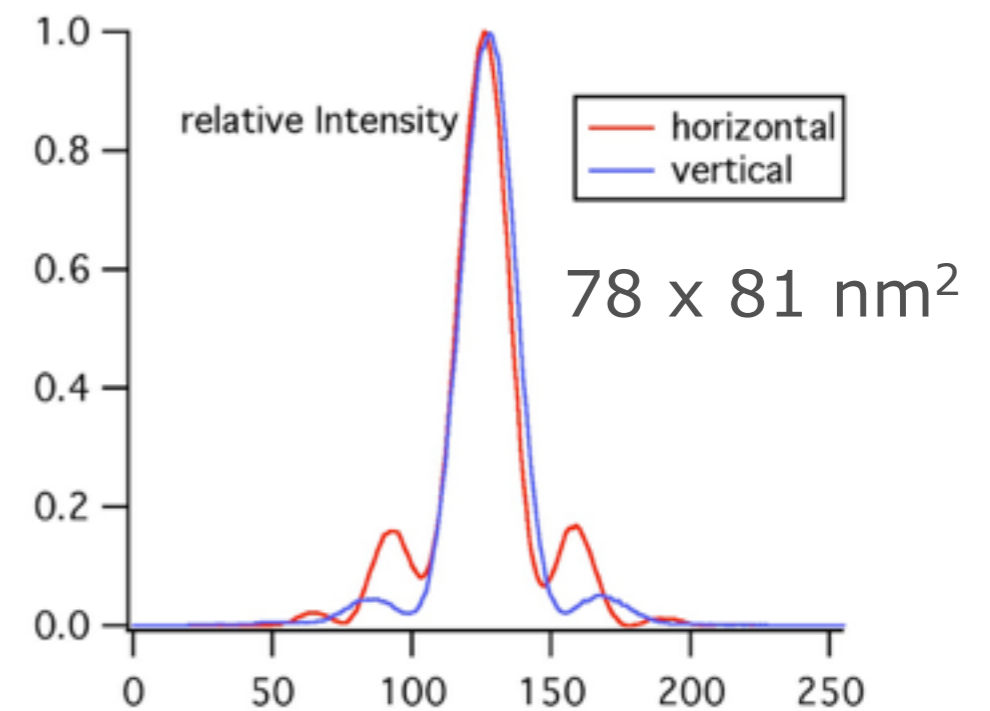
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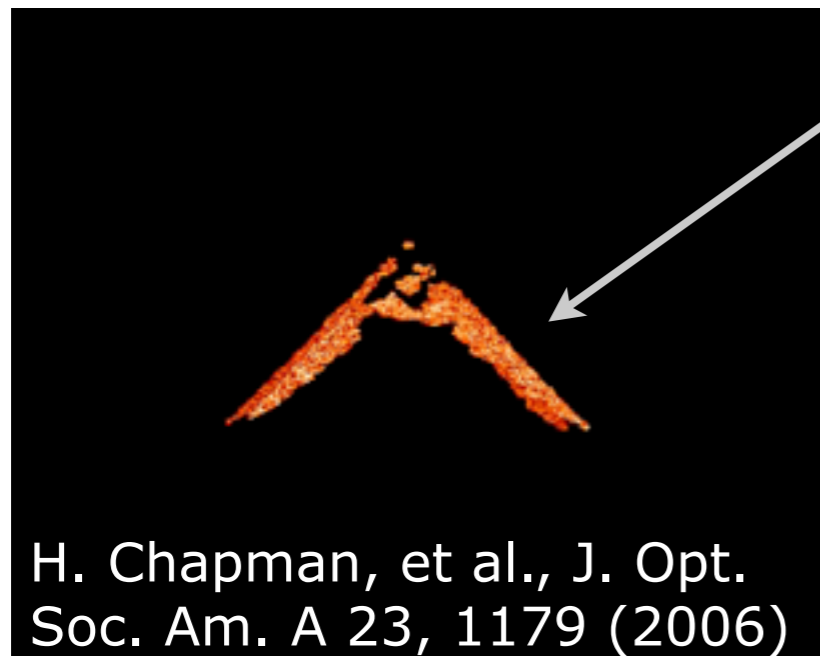
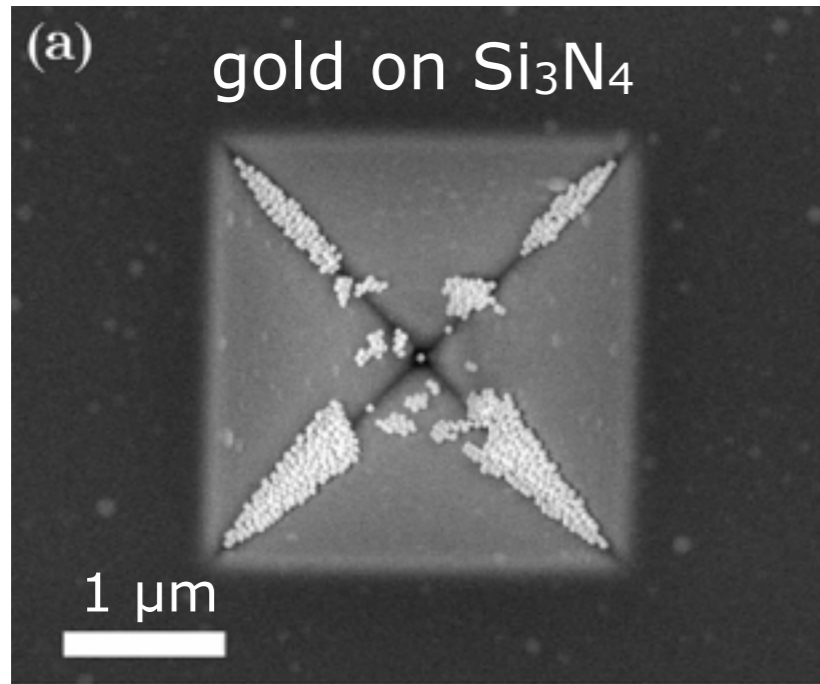
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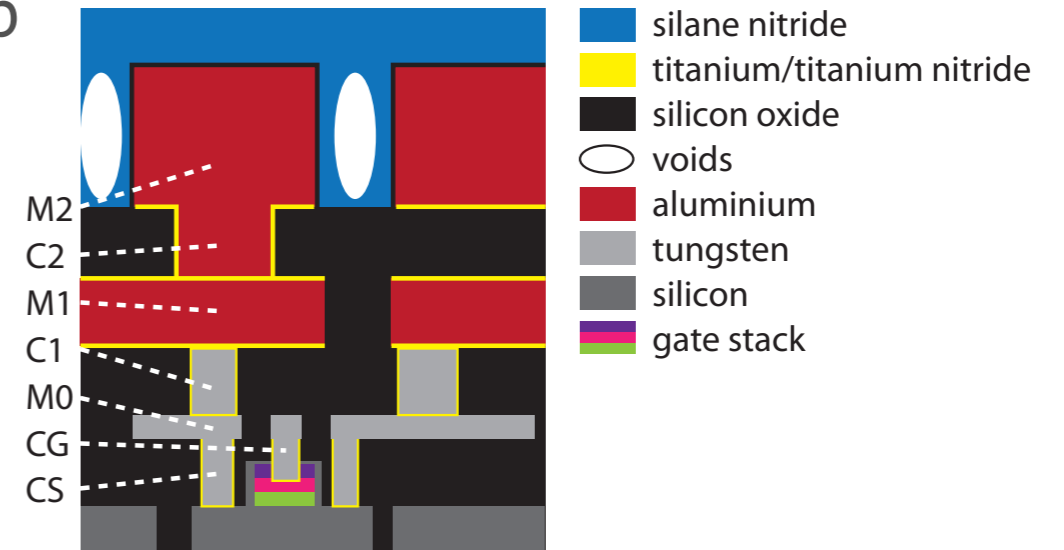
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Contrast in Coherent X-Ray Diffraction Imaging

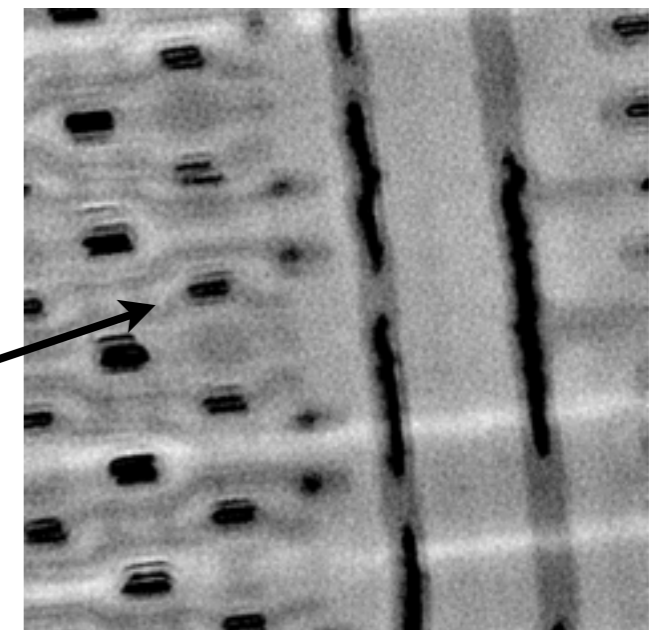


Microchip



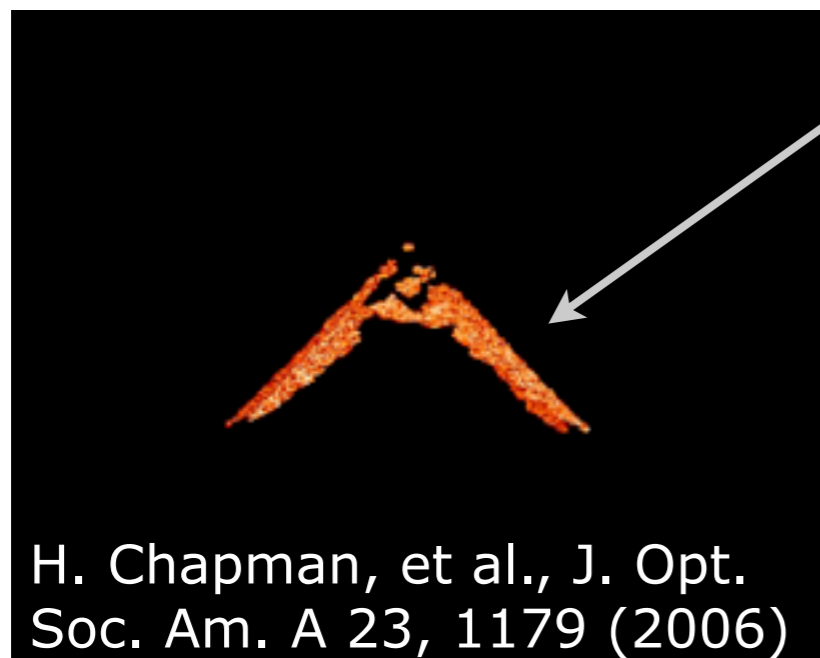
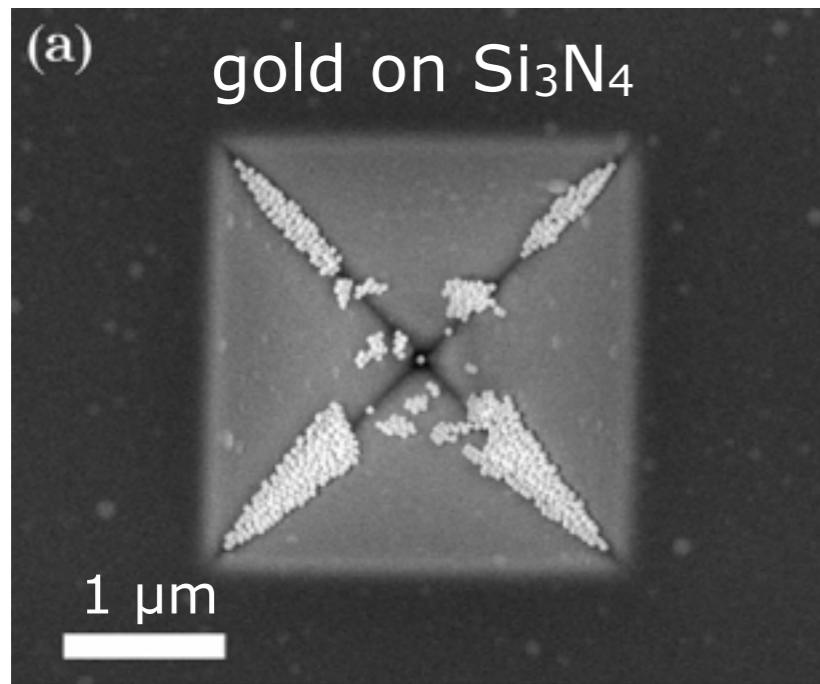
Au particles,
only!
No membrane!

Only tungsten!
Where is the
Al, Si, ... ?

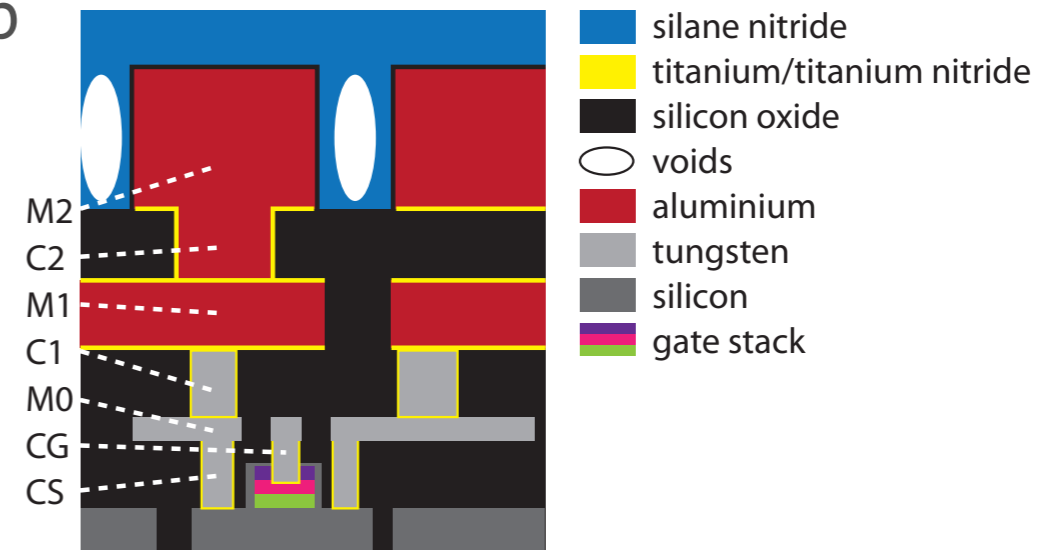


A. Schropp, et al., J. Microscopy, **241**(1), 9 (2011)

Contrast in Coherent X-Ray Diffraction Imaging

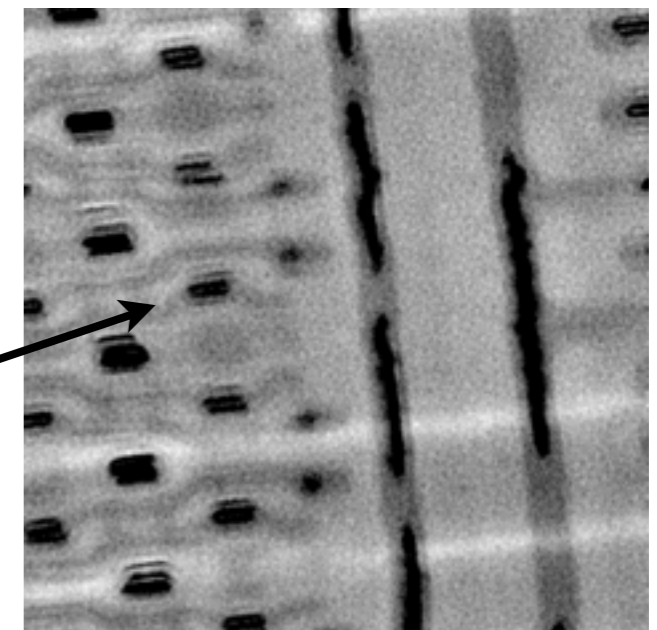


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Signal From Sample vs. Signal From Detail

Signal in a given detector pixel:

$$P(\vec{q}) = F(\vec{q}) \cdot \Delta t = I_c \int_{\Delta\Omega} |\psi_d + \psi_r|^2 d\Omega \cdot \Delta t$$

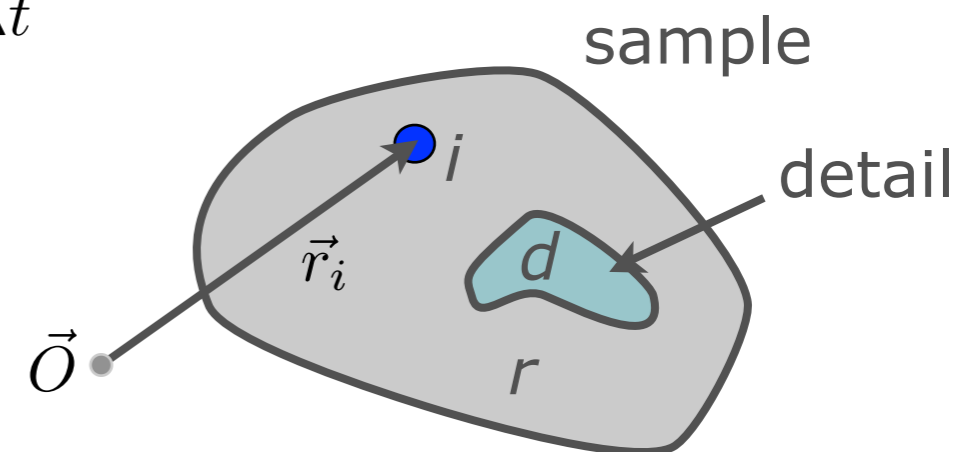
$$\psi_d = -r_0 p(\theta) \sum_{i \in d} f_i(\vec{q}) e^{-i\vec{q} \cdot \vec{r}}$$

$$= I_c \int_{\Delta\Omega} (|\psi_d|^2 + 2\Re(\psi_d \psi_r) + |\psi_r|^2) d\Omega \cdot \Delta t$$

I_c : coherent flux density

$\Delta\Omega$: solid angle of detector pixel

Δt : exposure time



Detail feature detectable (necessary condition) if

$$\left. \begin{array}{l} 2\Re(\psi_d \psi_r) \quad (\text{heterodyne}) \\ \text{or} \\ |\psi_d|^2 \quad (\text{homodyne}) \end{array} \right\} \geq \alpha \times \text{larger than shot noise from } |\psi_r|^2$$

$\alpha = 5 \quad (\text{Rose criterion})$

Signal From Sample vs. Signal From Detail

Signal-to-background considerations:

Feature can at best be detected when it can be imaged by itself!

$$I_c |\psi_d|^2 \Delta\Omega_d \cdot \Delta t \geq \frac{\alpha^2}{4}$$

necessary condition!

$\Delta\Omega_d$: size of Shannon pixel
for given feature

scattering amplitude of feature:

$$\psi_d = -r_0 p(\theta) \sum_{i \in d} f_i(\vec{q}) e^{-i\vec{q} \cdot \vec{r}}$$

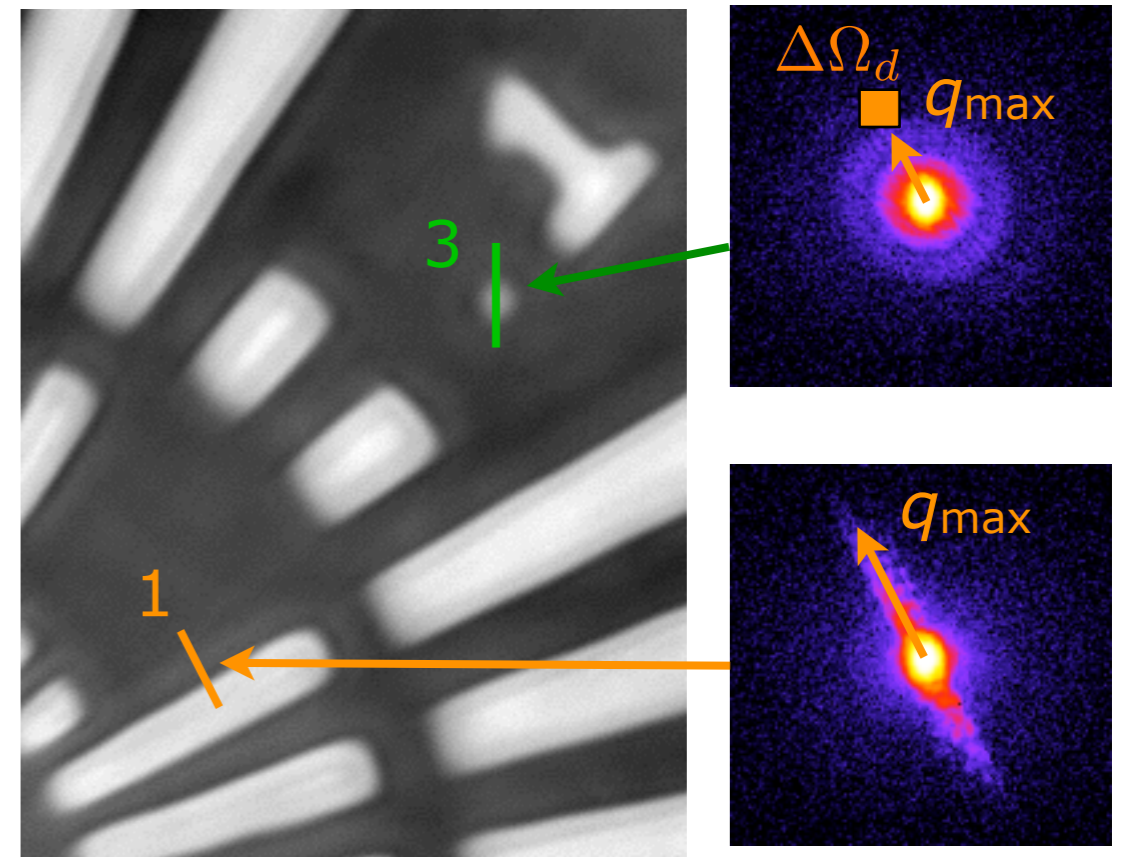
Scattering cross section of feature:

$$\left(\frac{d\sigma}{d\Omega} \right)_d = |\psi_d|^2$$

Detecting a feature inside an object

$$\underbrace{I_c \Delta t}_{\text{intensity}} \cdot \underbrace{|\psi_d|^2 \Delta \Omega_d}_{\text{structure factor}} \geq \frac{\alpha^2}{4}$$

~ structure factor of feature:



Detecting a feature inside an object

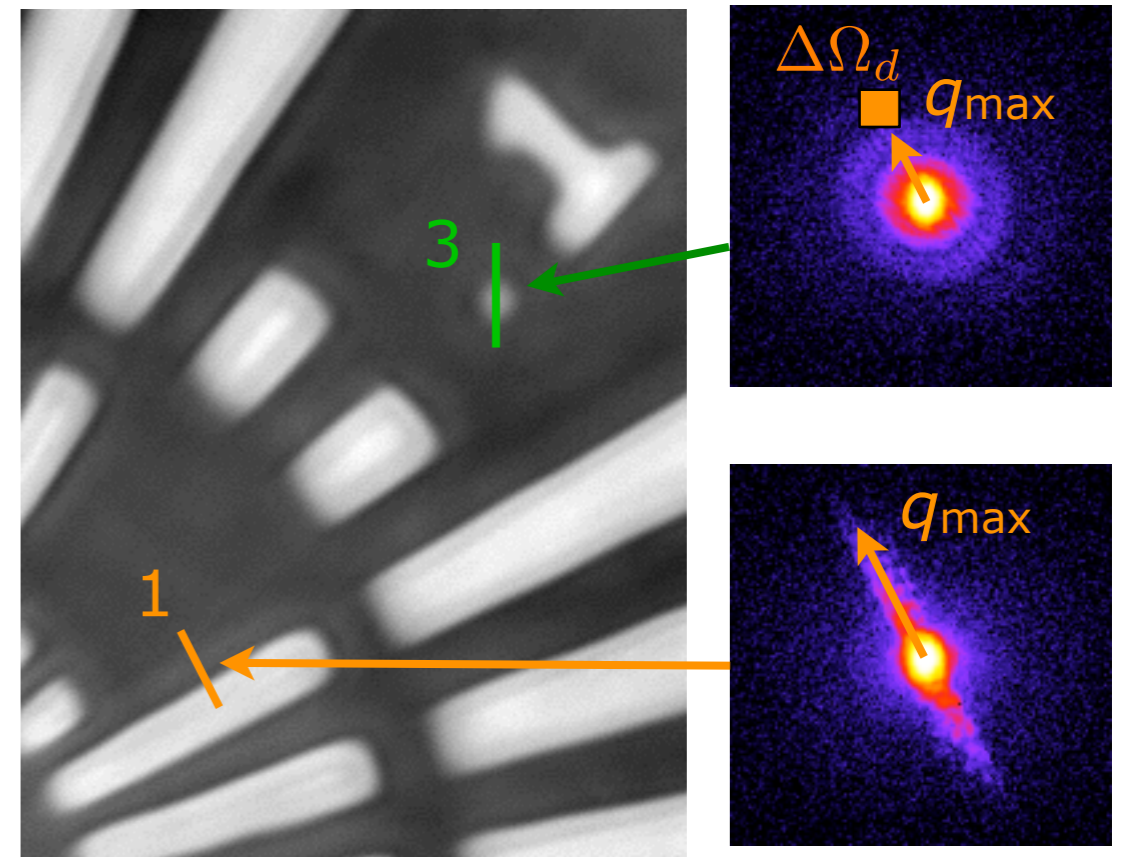
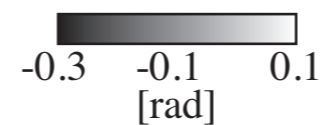
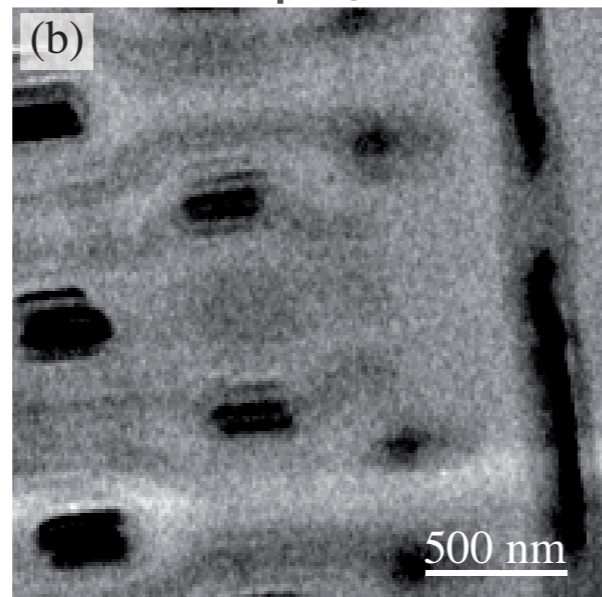
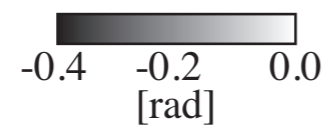
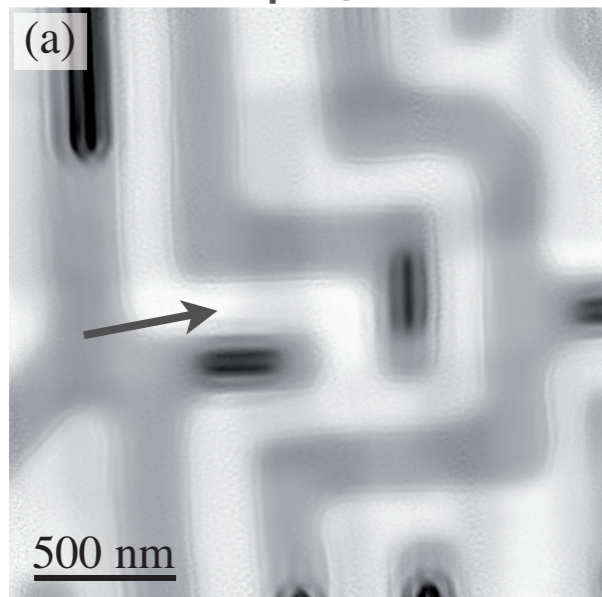
$$\underbrace{I_c \Delta t}_{\text{coherent fluence on feature:}} \cdot \underbrace{|\psi_d|^2 \Delta \Omega_d}_{\sim \text{structure factor of feature:}} \geq \frac{\alpha^2}{4}$$

coherent fluence on feature:

\sim structure factor of feature:

$6.7 \cdot 10^3 \text{ ph/nm}^2$

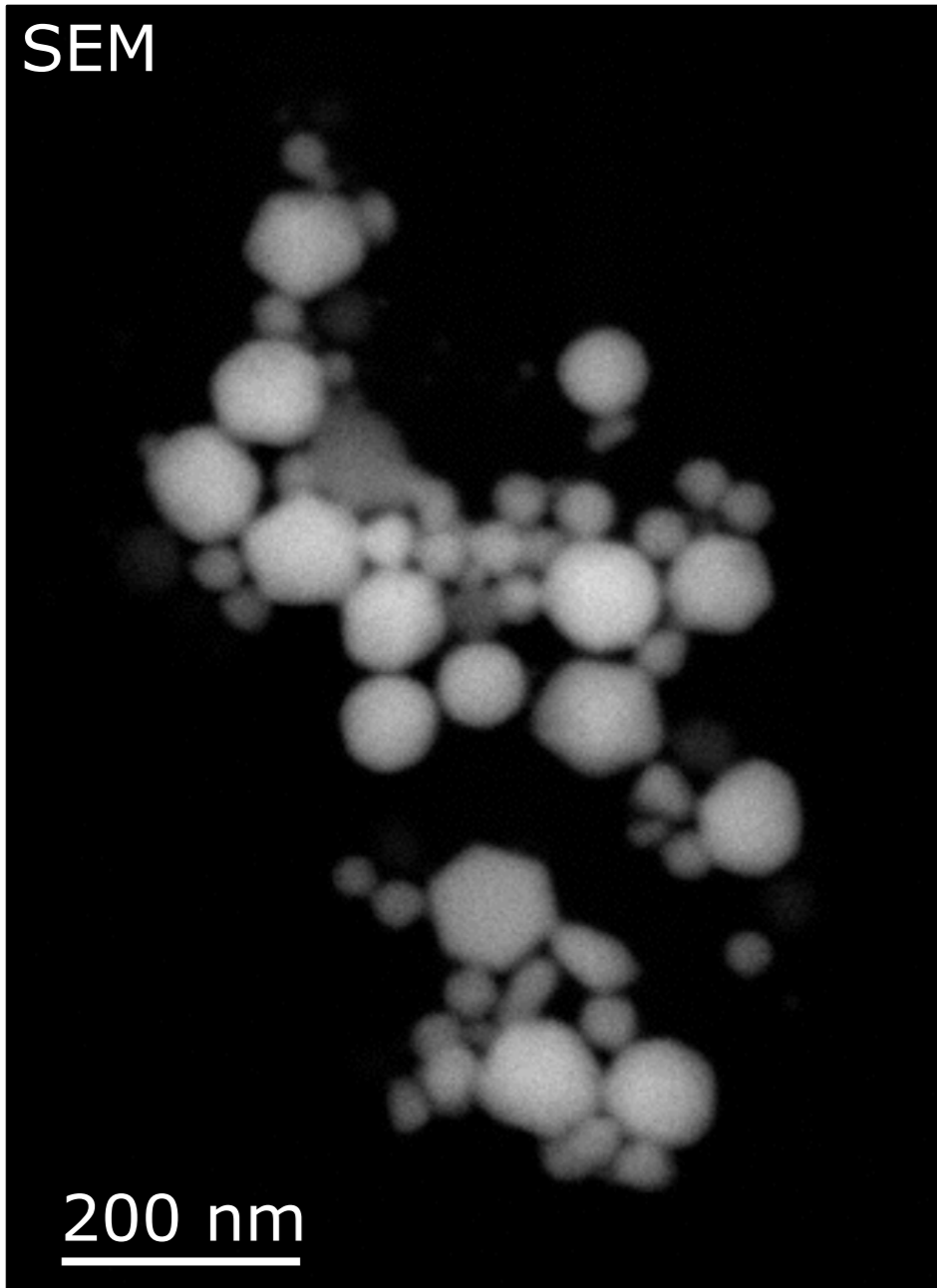
$3.9 \cdot 10^2 \text{ ph/nm}^2$



Ptychography: Sensitivity & Resolution

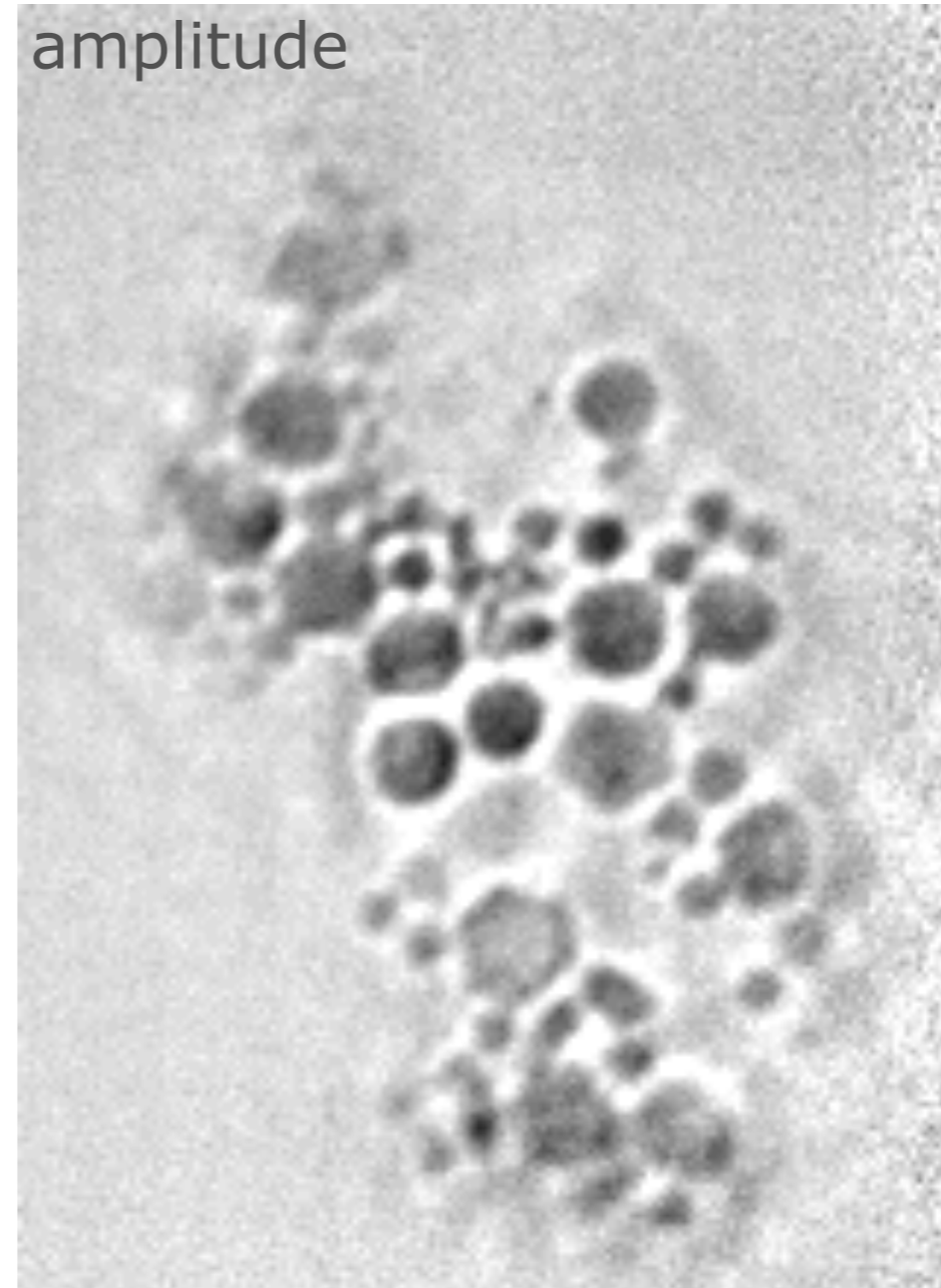
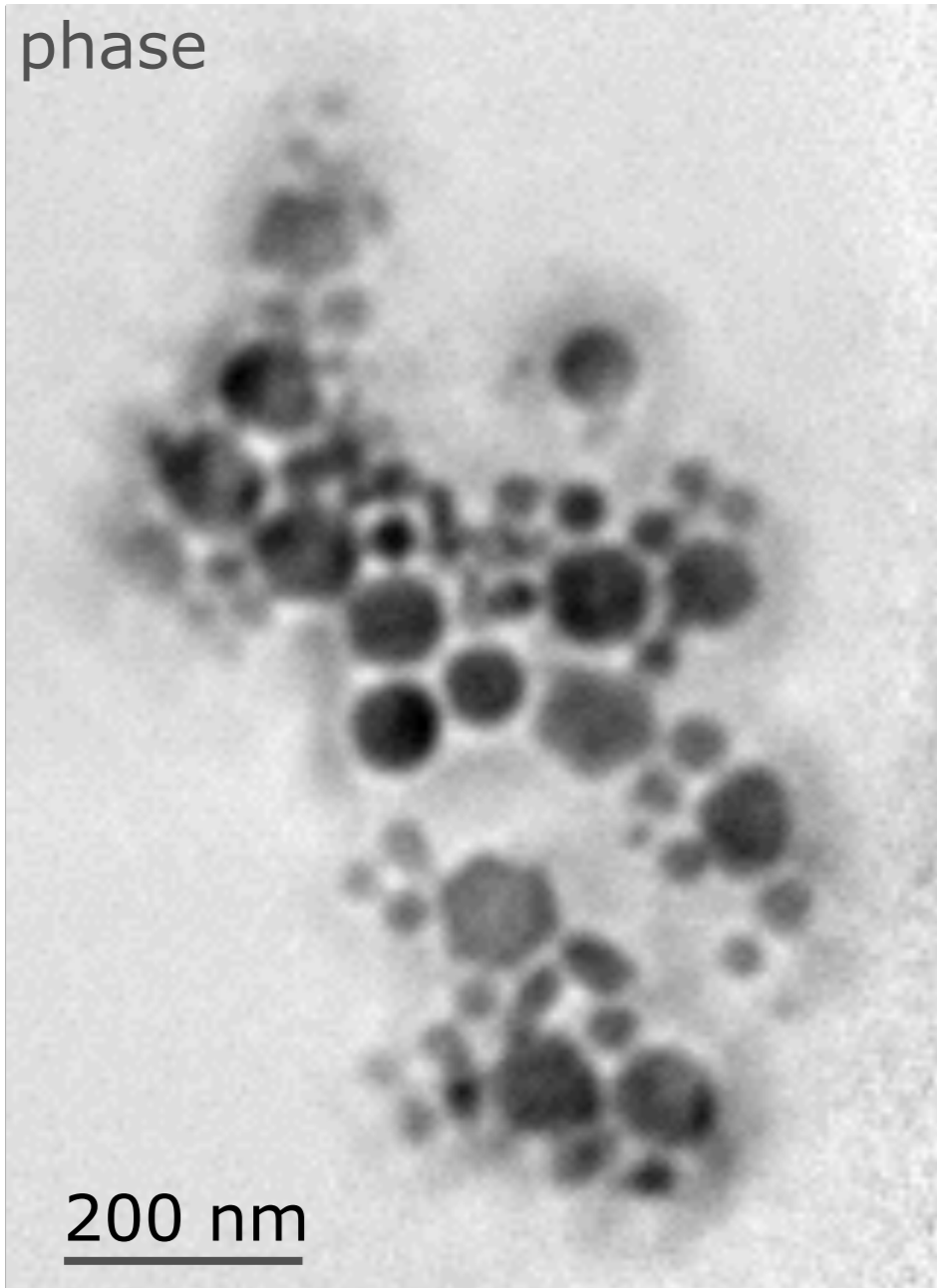
Sample: Pd, Pt, and Au particles

SEM



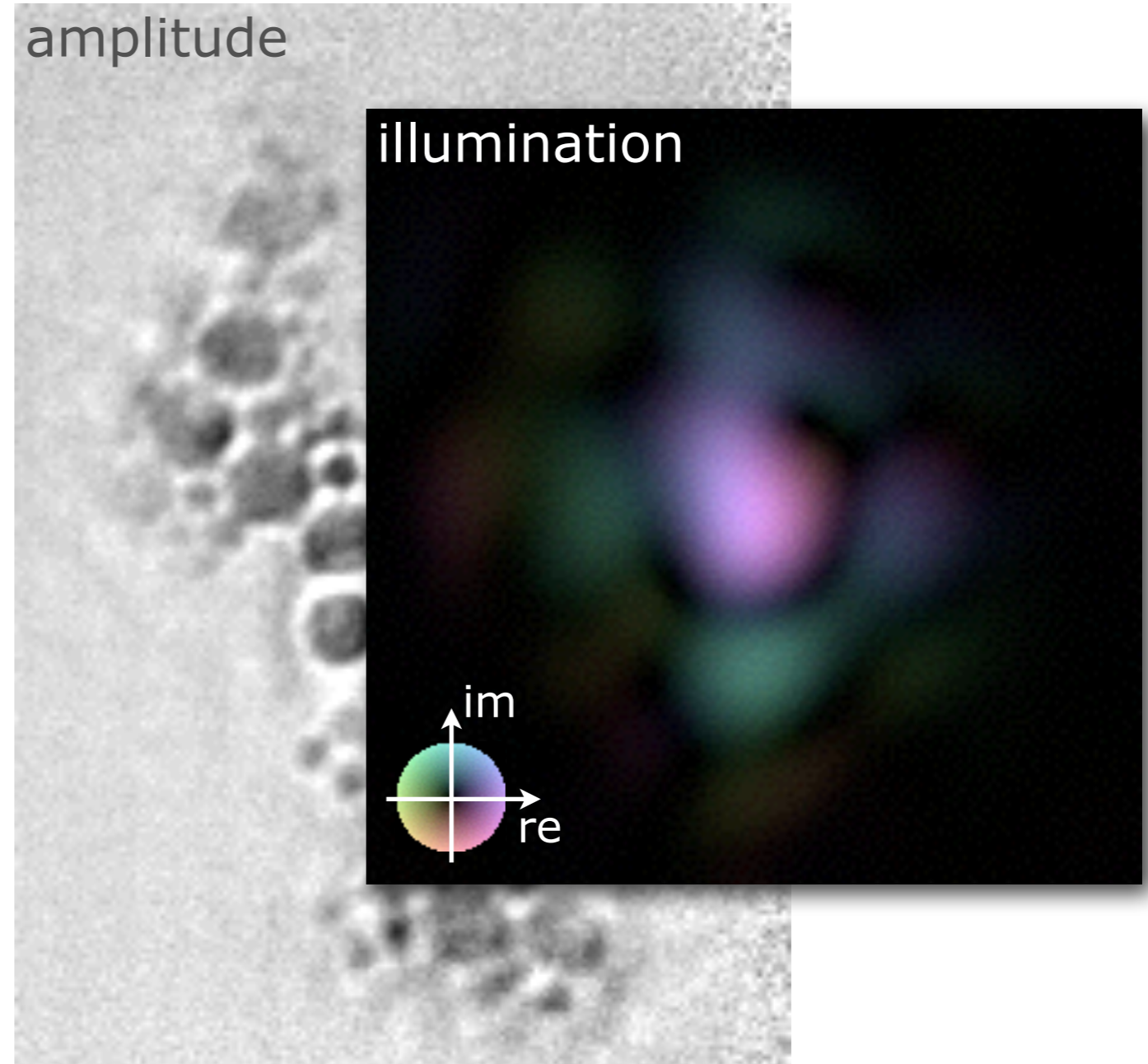
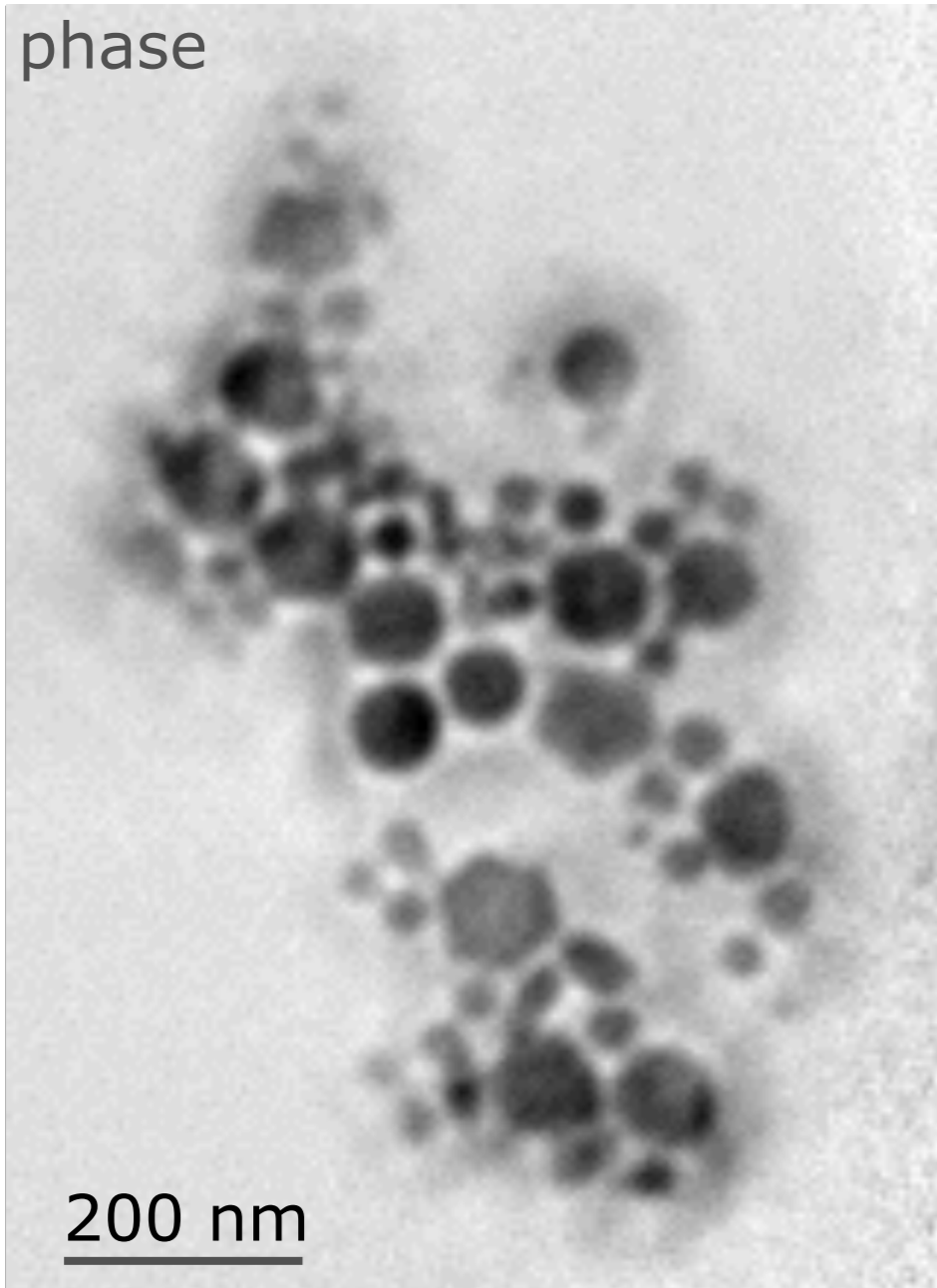
Ptychography: Sensitivity & Resolution

Sample: Pd, Pt, and Au particles



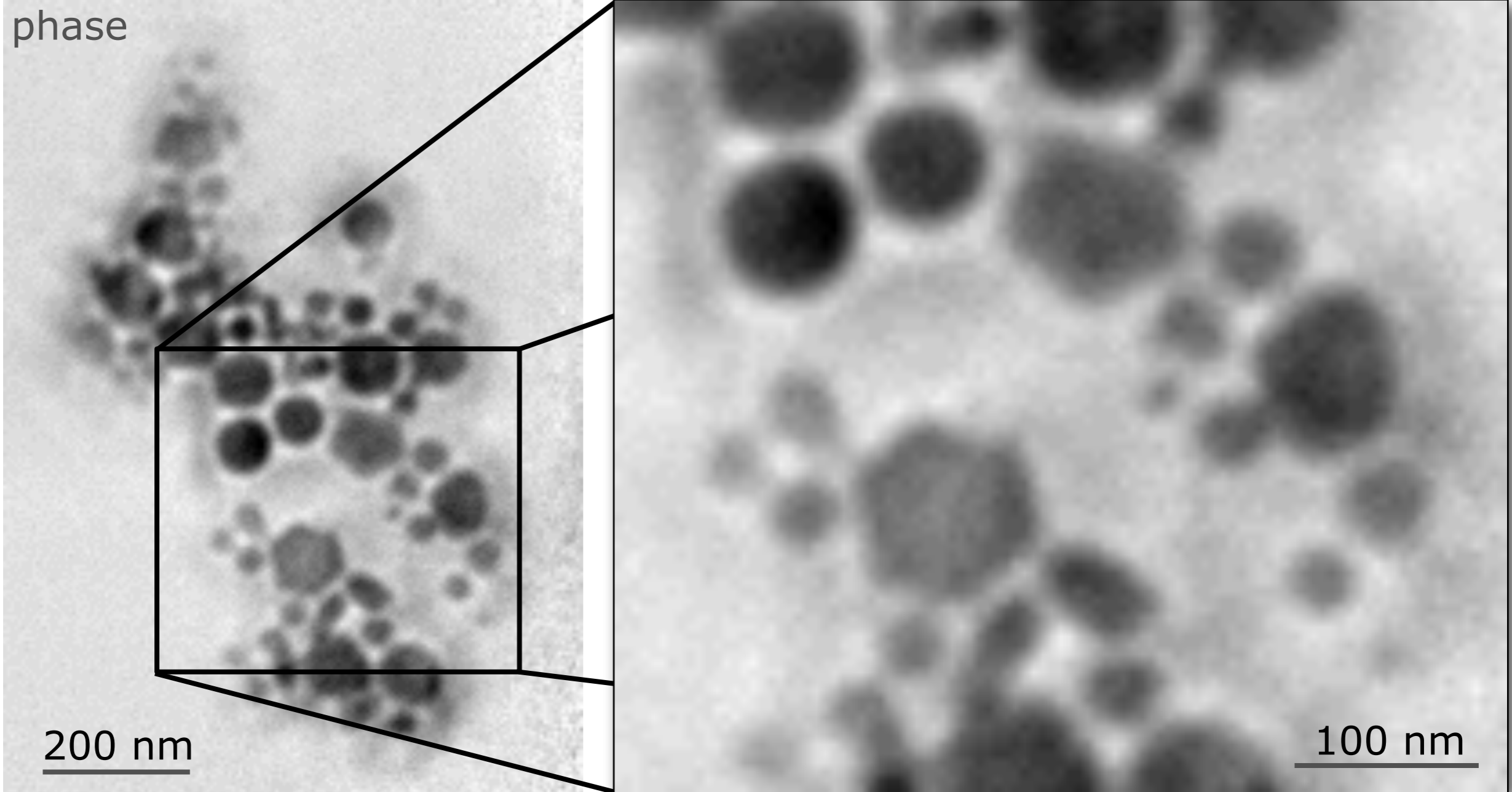
Ptychography: Sensitivity & Resolution

Sample: Pd, Pt, and Au particles



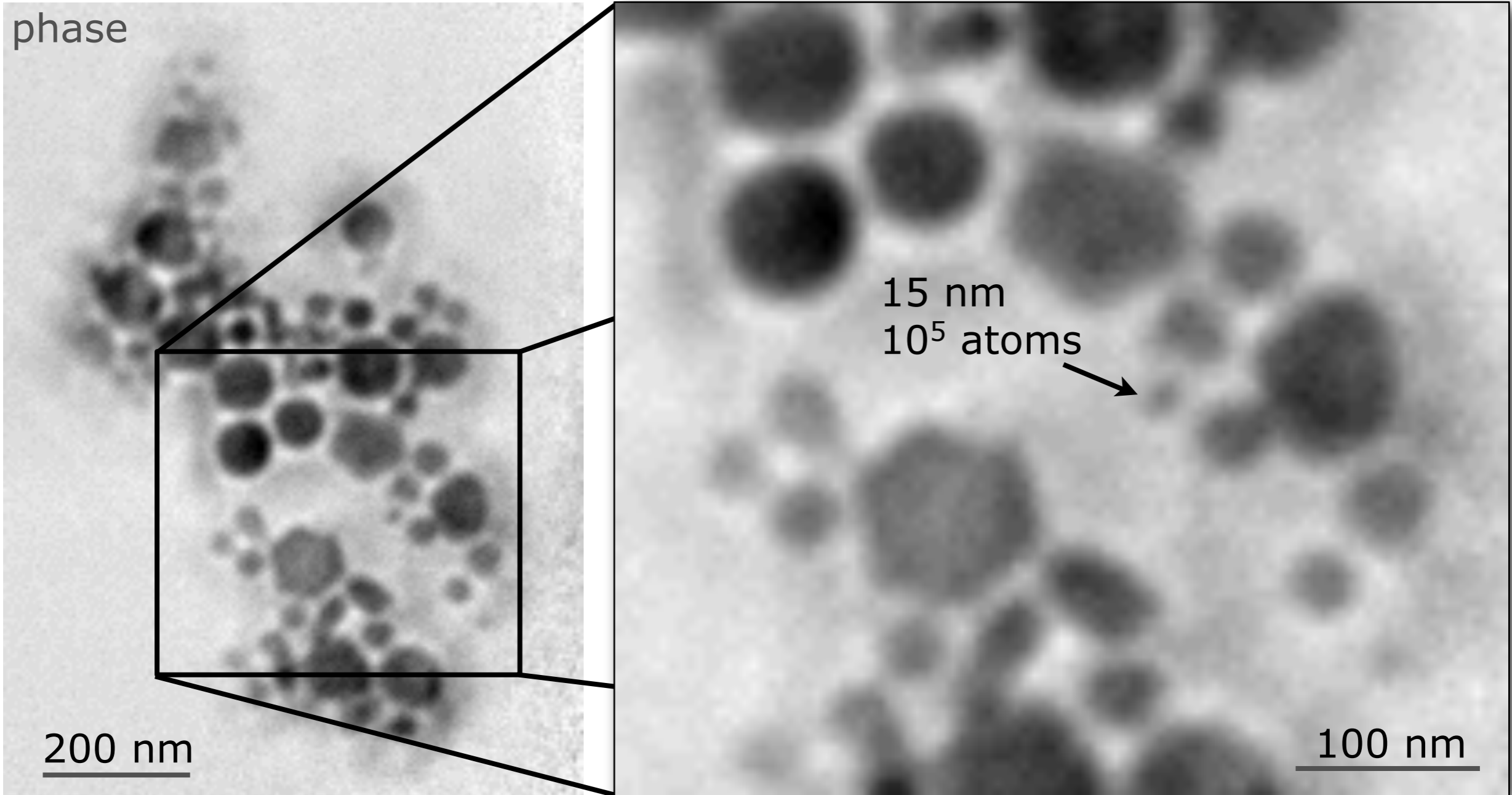
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Ptychography: Sensitivity & Resolution

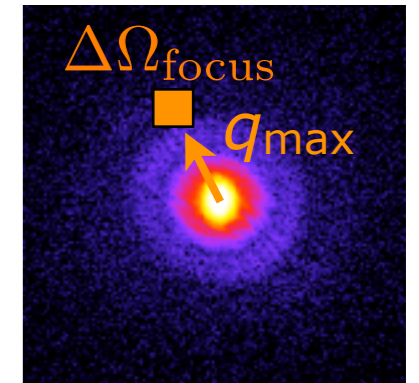
Sample: Pd, Pt, and Au particles



Locating a Feature at High Spatial Resolution

Signal from small feature in given speckle at high q_{\max} :

$$I_c \cdot t \cdot \frac{d\sigma}{d\Omega}(\vec{q}_{\max}) \cdot \Delta\Omega_{\text{focus}} \geq \frac{\alpha^2}{4}$$



- $I_c \cdot t$: coherent fluence on feature
- $\frac{d\sigma}{d\Omega}(\vec{q}_{\max})$: scattering cross section of feature at highest q
- $\Delta\Omega_{\text{focus}}$: Speckle size defining a piece of information in reciprocal space


Figure of merit of x-ray microscope:

$$I_c \cdot t \cdot \Delta\Omega_{\text{focus}} \quad \text{coherent fluence per entropy in diff. pattern}$$

Locating a Feature at High Spatial Resolution

Coherent fluence:

$$I_c \cdot t = \frac{F_c}{A} \cdot T \cdot t \quad F_c \propto Br \cdot \lambda^2 \cdot \frac{\Delta E}{E} \quad \text{coherent flux}$$



 illuminated area
 optic's transmission

Diffraction limited focus:


$$I_c \cdot t \propto Br \cdot \frac{\Delta E}{E} \cdot \underbrace{NA^2}_{\text{optic}} \cdot T \cdot t$$



 source
 optic

Size of speckle in diffraction pattern:

$$\Delta\Omega_{\text{focus}} = \pi \frac{\lambda^2}{4d_t^2} = \pi NA^2$$


 optic

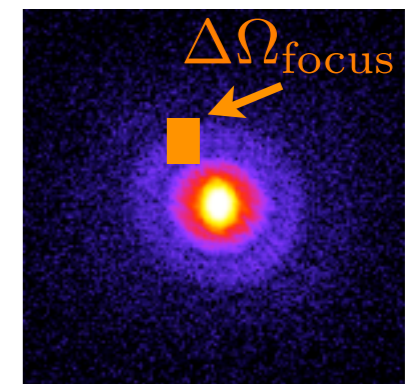
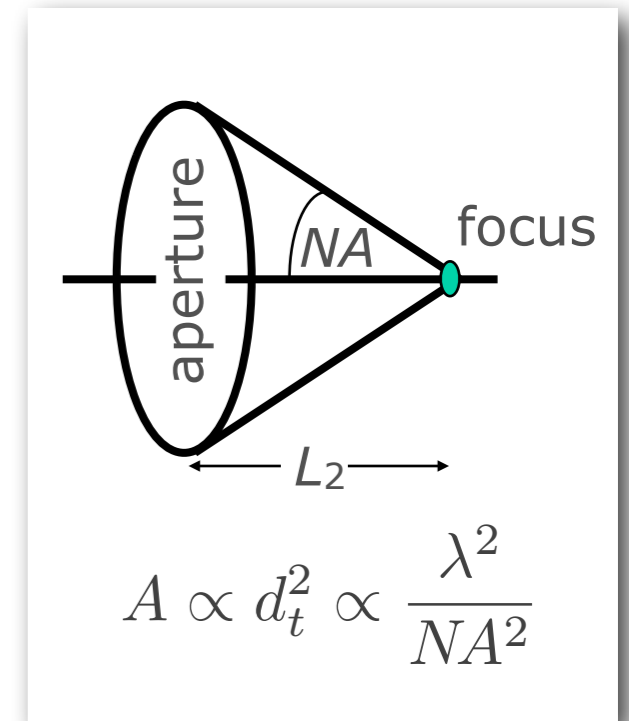


Figure of Merit of X-Ray Microscope

Signal from small feature in given speckle at high q_{\max} :

$$I_c \cdot t \cdot \frac{d\sigma}{d\Omega}(\vec{q}_{\max}) \cdot \Delta\Omega_{\text{focus}} \propto \underset{\substack{\uparrow \\ \text{source}}}{Br} \cdot \frac{\Delta E}{E} \cdot \underbrace{NA^4 \cdot T}_{\substack{\uparrow \\ \text{optic}}} \cdot t$$

Improve scanning coherent diffraction microscope:

- 🌐 upgrade the source:

- diffraction limited storage ring

- 🌐 improve optic:

- $\propto NA^4$ strong dependence on numerical aperture!

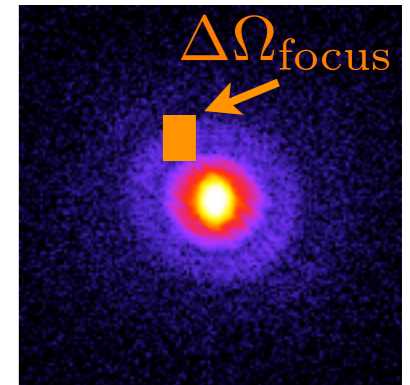
- transmission

Atomic Resolution?

Have sufficiently many scattered photons in speckle at large q !

Size of speckle in diffraction pattern:

$$\Delta\Omega_{\text{focus}} = \pi \frac{\lambda^2}{4d_t^2} = \pi NA^2 \quad NA: \text{numerical aperture of optic}$$



given example:

$$\Delta\Omega_{\text{focus}} \approx 10^{-6} \text{ srad}$$

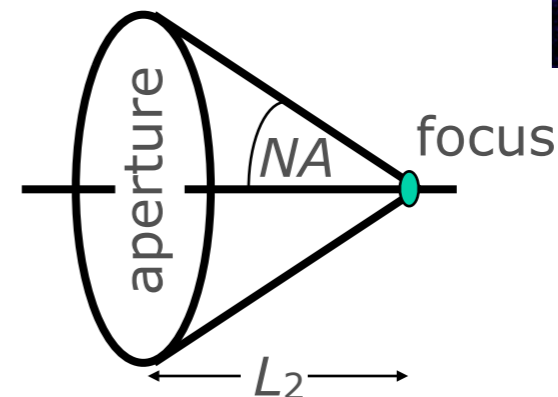
elastic scattering of gold atom to 1 Å:

$$I_c \frac{d\sigma}{d\Omega} t = 0.4 \cdot 10^{-3} \text{ srad}^{-1}$$

Current experiment:

$$I_c \cdot t \cdot \frac{d\sigma}{d\Omega} \Delta\Omega_{\text{focus}} \approx 4 \cdot 10^{-10}$$

is about 10 orders of magnitude off!!!



Route to Atomic Resolution...

Coherent fluence:

$$I_c \cdot t = \frac{F_c}{A} \cdot T \cdot t \quad F_c \propto Br \cdot \lambda^2 \cdot \frac{\Delta E}{E} \quad \text{coherent flux}$$

↑
↑
↑

illuminated area
optic's transmission

Ways to increase fluence:

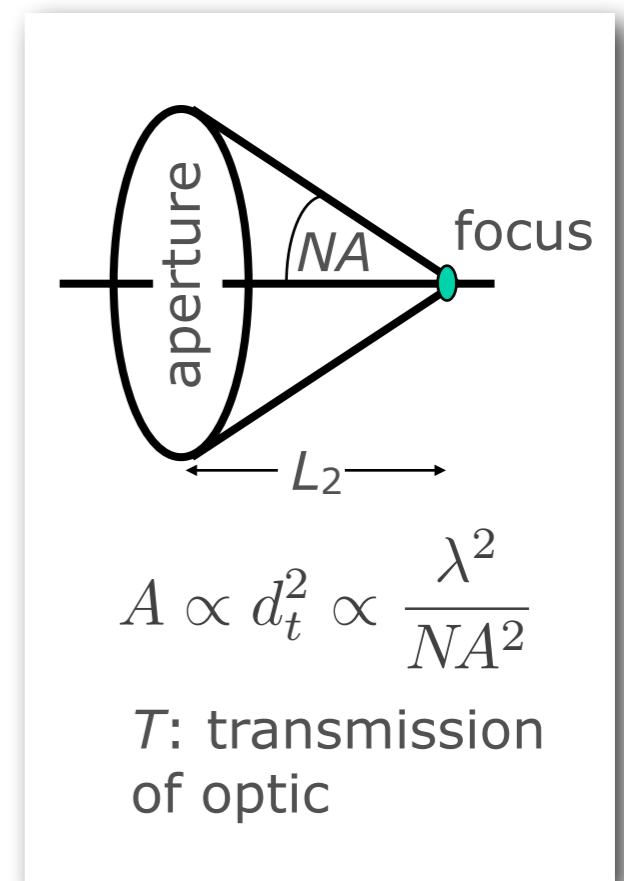
- 🌀 increase brilliance Br
- 🌀 decrease illuminated area A
- 🌀 improve transmission T of optic
- 🌀 longer exposure t

Diffraction limited focus:

$$I_c \cdot t \propto Br \cdot \frac{\Delta E}{E} \cdot \underbrace{NA^2 \cdot T}_{\text{optic}} \cdot t$$

↑
↑

source
optic



Route to Atomic Resolution...

Signal in diffraction pattern:

$$I_c \cdot t \cdot \frac{d\sigma}{d\Omega} \cdot \Delta\Omega_{\text{focus}} \propto \underset{\substack{\uparrow \\ \text{source}}}{Br} \cdot \frac{\Delta E}{E} \cdot \underbrace{NA^4 \cdot T \cdot t}_{\substack{\uparrow \\ \text{optic}}}$$

speckle size:

$$\Delta\Omega_{\text{focus}} = \pi \frac{\lambda^2}{4d_t^2} = \pi NA^2$$

fluence:

$$I_c \cdot t \propto Br \cdot \frac{\Delta E}{E} \cdot NA^2 \cdot T \cdot t$$

Improvements (compared to current experiment):

- upgraded sources (DLSR):

$$Br \rightarrow \times 40 - \times 1000 \quad 10 - 10^3$$

- improve optic:

$$T \rightarrow \times (7 \cdot 100) \quad 10 - 10^3$$

efficiency relaxing spatial filtering of source

$$NA \rightarrow \times 10 \quad (10 \text{ nm focus}) \quad \frac{10^4}{10^{10}}$$

overall improvement: 10^{10}

Route to Atomic Resolution...

atomic resolution not completely out of reach!

- requires diffraction limited storage ring
increase in brilliance & matching of coherence length
(Thibault, Menzel, Nature **494**, 68 (2013))
- significant gain by extreme focusing

$$\propto NA^4$$

Here: optical aspects covered!

Other issues:

- **modification/destruction** of the sample by imaging
- stability of mechanics & beam
- background (e. g., Compton scattering)

Holy Grail in X-Ray Microscopy

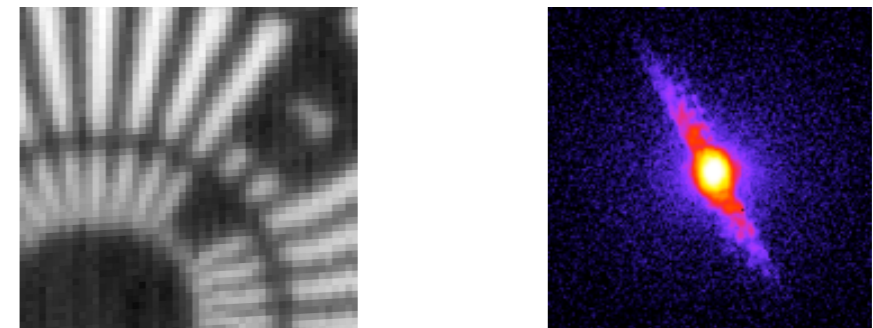
In-situ quantitative measurement of physical properties of matter on

- all relevant length scales and
- all relevant time scales!

Key technology: brilliant coherent x-rays with time structure

Fusion of real and reciprocal space:

speckle size matches
real space resolution



- access to all length scales:
(in principle) from Å to millimeters

