

Discussion on Hosing Instability In the Blow-Out PWFA

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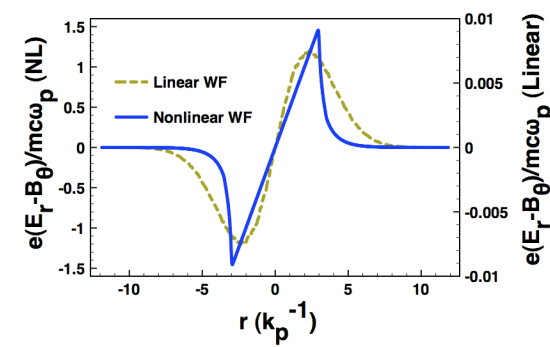
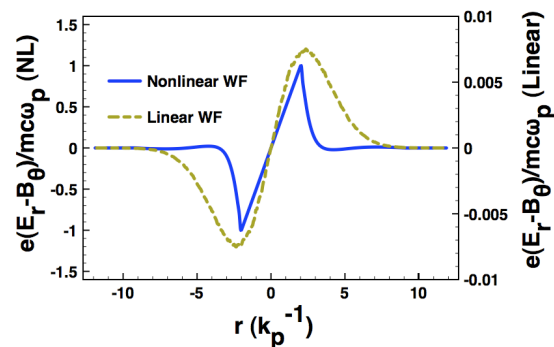
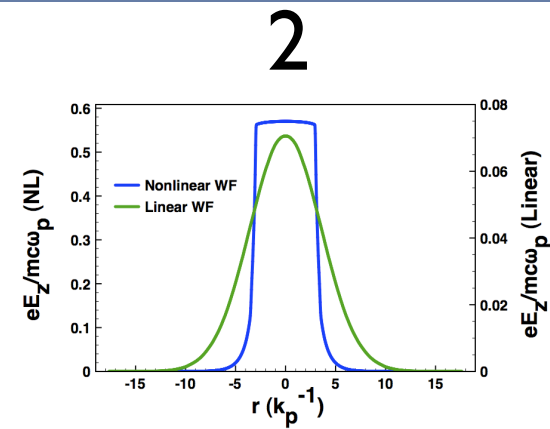
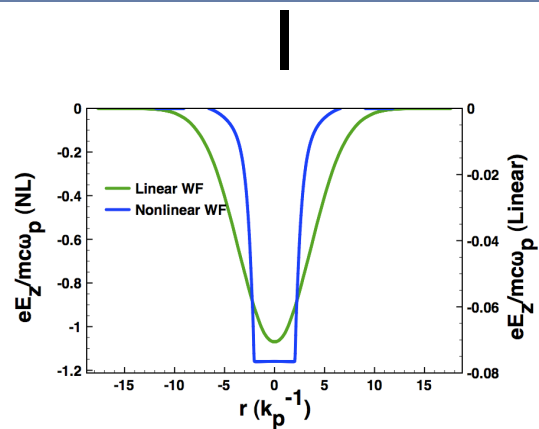
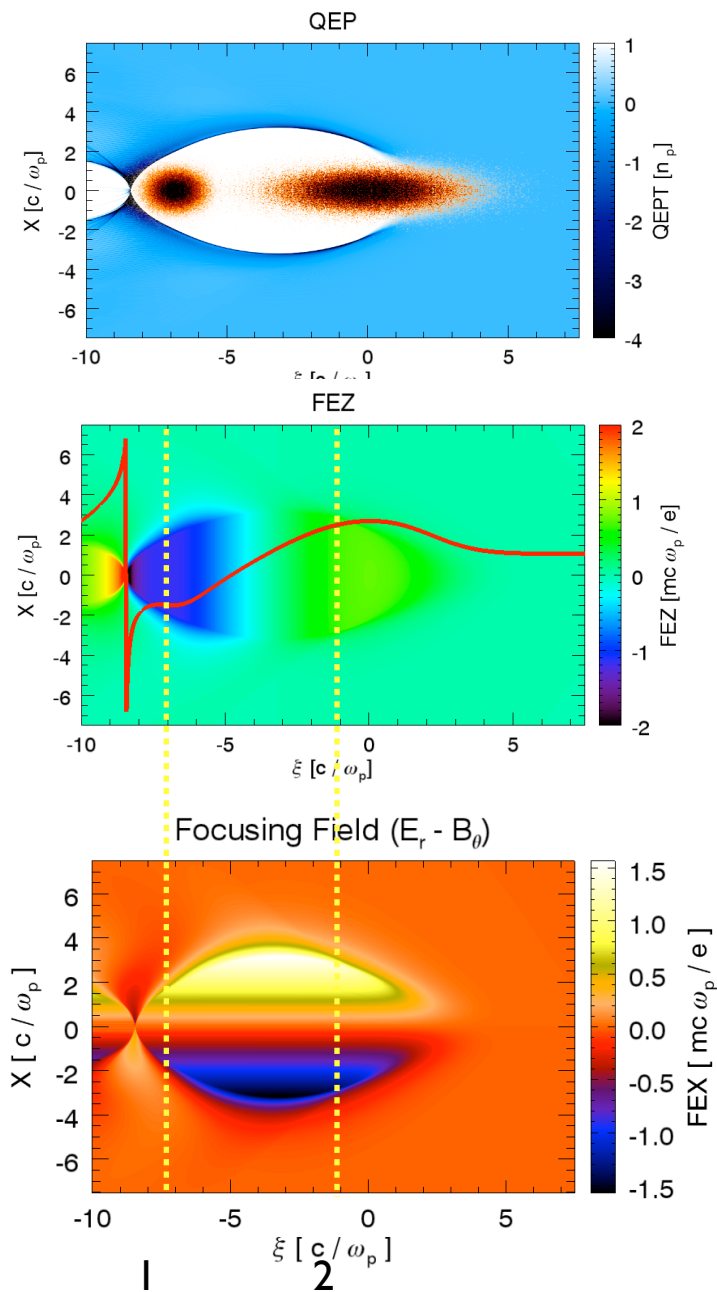
With help from Xinlu Xu, Lance Hildebrand and Warren Mori



PICKSC
<http://picksc.idre.ucla.edu>



FACET-II
Facility for Advanced Accelerator Experimental Tests



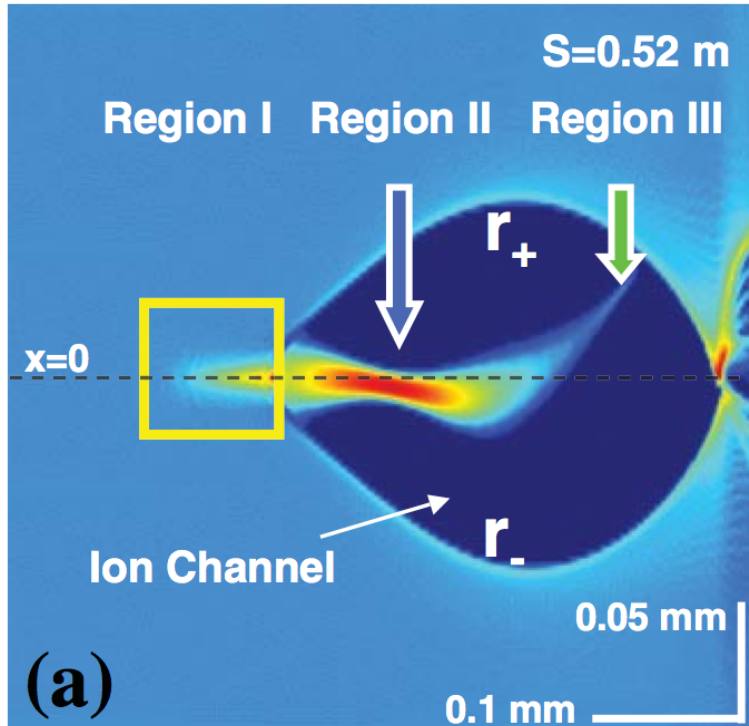
Superposition is Not Satisfied for Strong Beam Load.

Zeroth order problem: Beam Loading

* M. Tzoufras et. al., PRL 101, 145002 (2008)

First order problem: Beam Hosing

2* C. Huang et. al., PRL 99, 255001 (2007)



* C. Huang et. al., PRL 99, 255001 (2007)

$$\partial_s^2 x_b + k_\beta^2 x_b = k_\beta^2 x_c.$$

$$x_c'' + c_r c_\psi \omega_0^2 x_c = c_r c_\psi \omega_0^2 x_b$$

Nonlinear Equation!

$$k_\beta = k_p / \sqrt{2\gamma}, \quad \omega_0 = k_p / \sqrt{2}$$

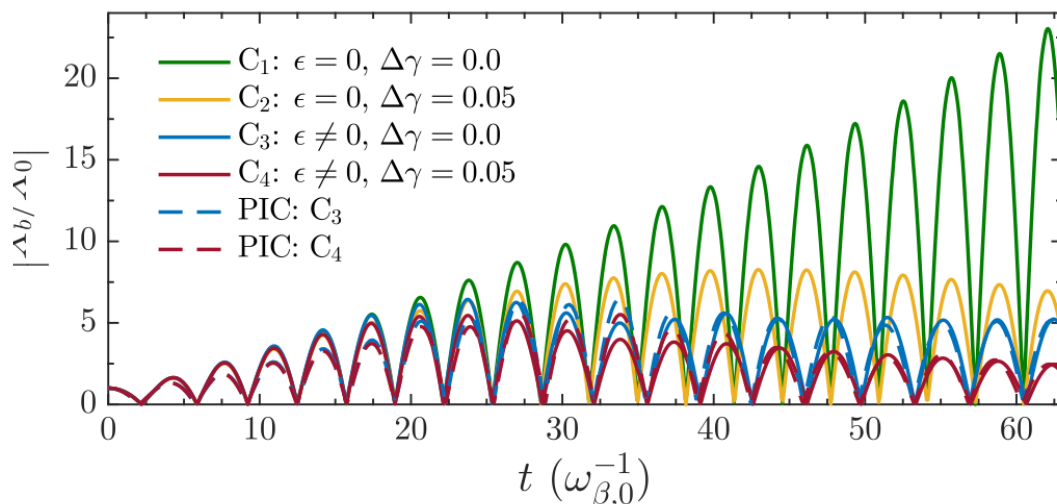
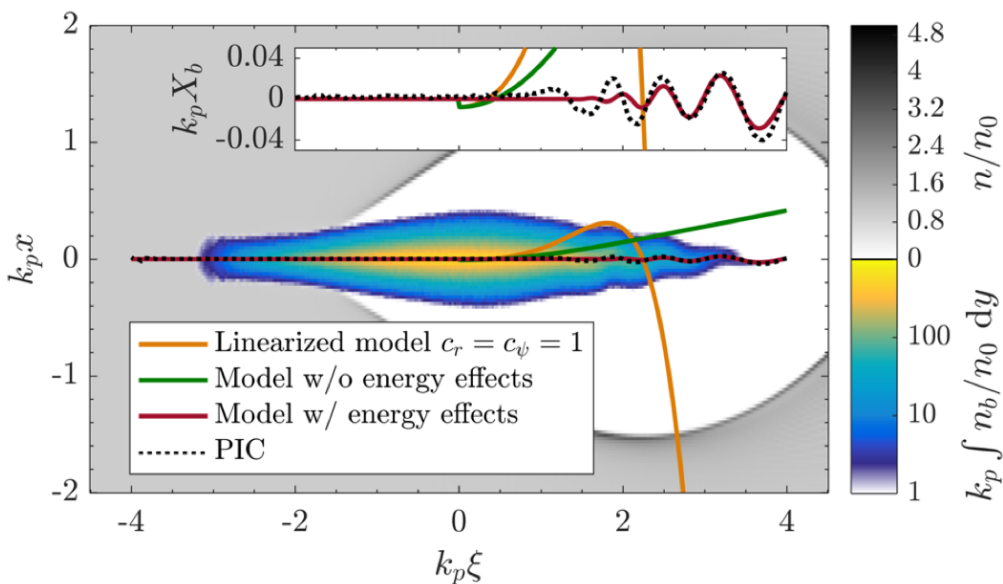
$$c_r \equiv n_b R_b^2 / r_0^2$$

$$c_\psi \equiv 1 / (1 + \psi_0)$$

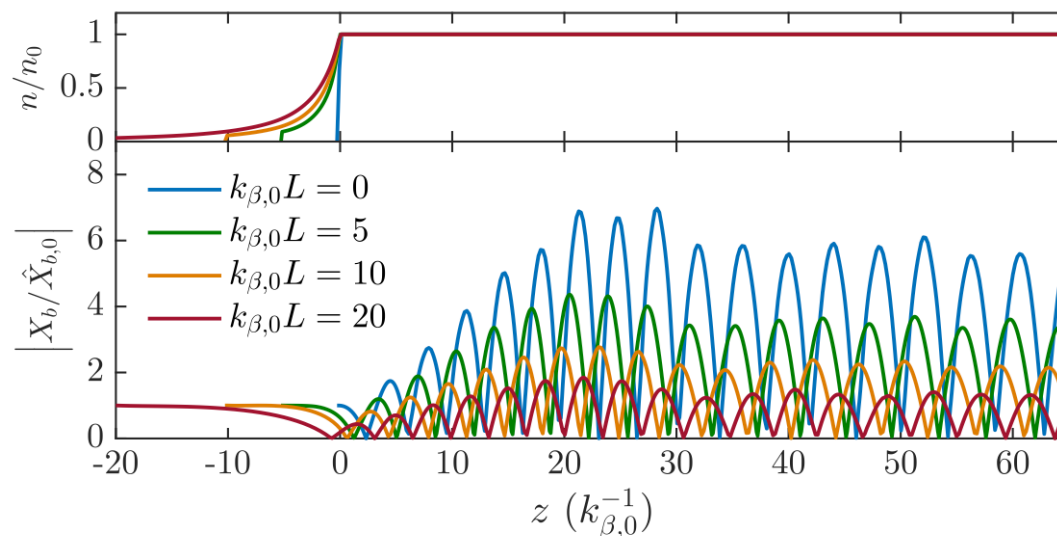
E-folding for the Growth Rate

$$1.3 [c_r c_\psi (k_\beta s) (\omega_0 \xi)^2]^{1/3}$$

BNS Damping Longitudinally correlated energy spread



$$\frac{\partial^2 X_b}{\partial t^2} + \frac{\overline{\omega_\beta^2}}{\omega_{\beta,0}} (\epsilon + \kappa_1 \Delta\gamma^2) \frac{\partial X_b}{\partial t} + \overline{\omega_\beta^2} (1 + \kappa_2 \Delta\gamma^2) (X_b - X_c) = 0$$



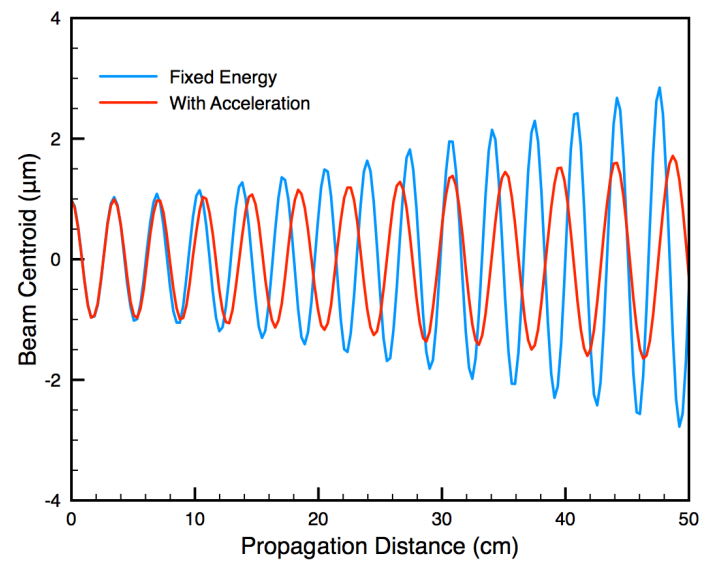
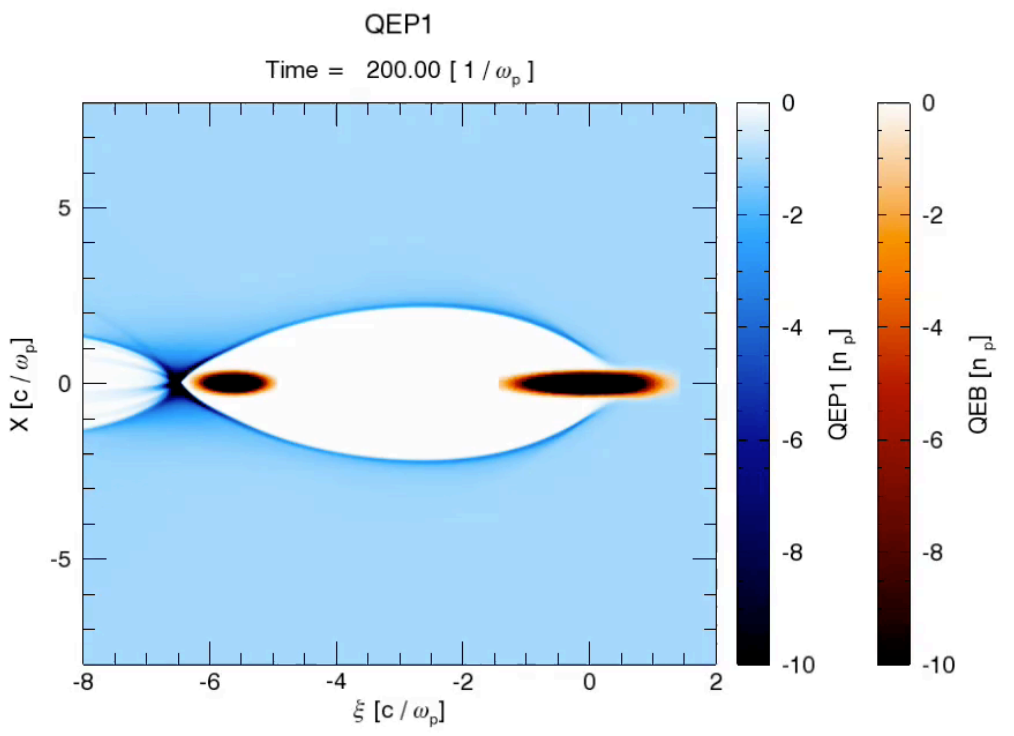
* T. Mehrling et. al., PRL 118, 174801 (2017)

What about the trailing beam?

Drive Beam: $E = 10$ GeV, $I_{\text{peak}} = 15$ kA
 $\sigma_r = 3.65$ μm , $\sigma_z = 12.77$ μm ,
 $N = 1.0 \times 10^{10}$ (1.6 nC), $\epsilon_N = 50$ μm

Trailing Beam: $E = 10$ GeV, $I_{\text{peak}} = 9$ kA
 $\sigma_r = 3.65$ μm , $\sigma_z = 6.38$ μm ,
 $N = 4.33 \times 10^9$ (0.69 nC), $\epsilon_N = 50$ μm
 (transversely offset by 1 μm)

Distance between two bunches: 150 μm
Plasma Density: 4.0×10^{16} cm^{-3}



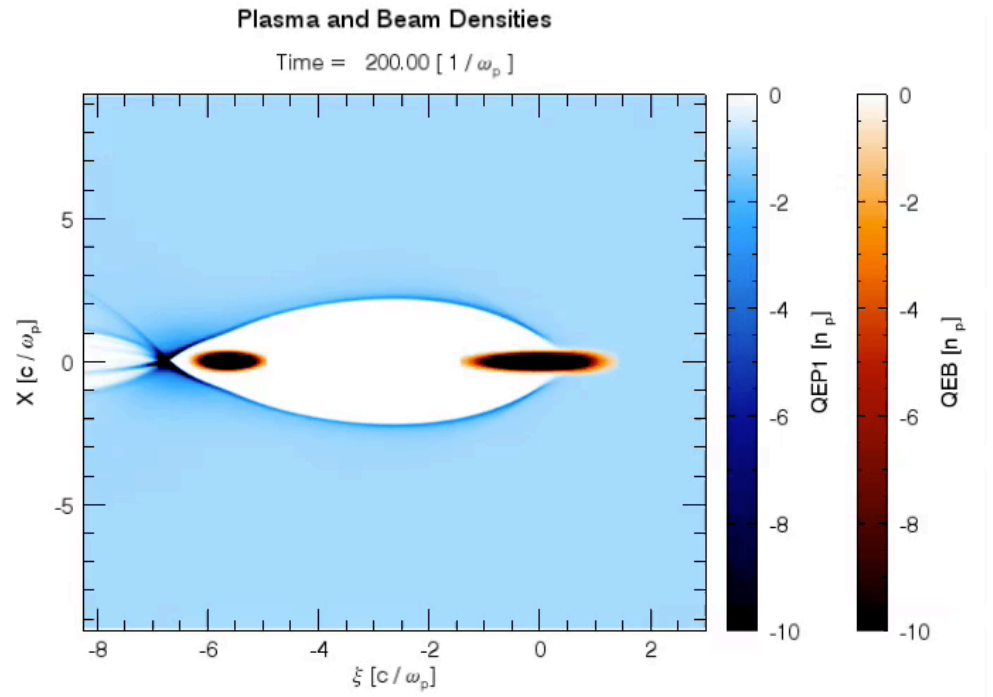
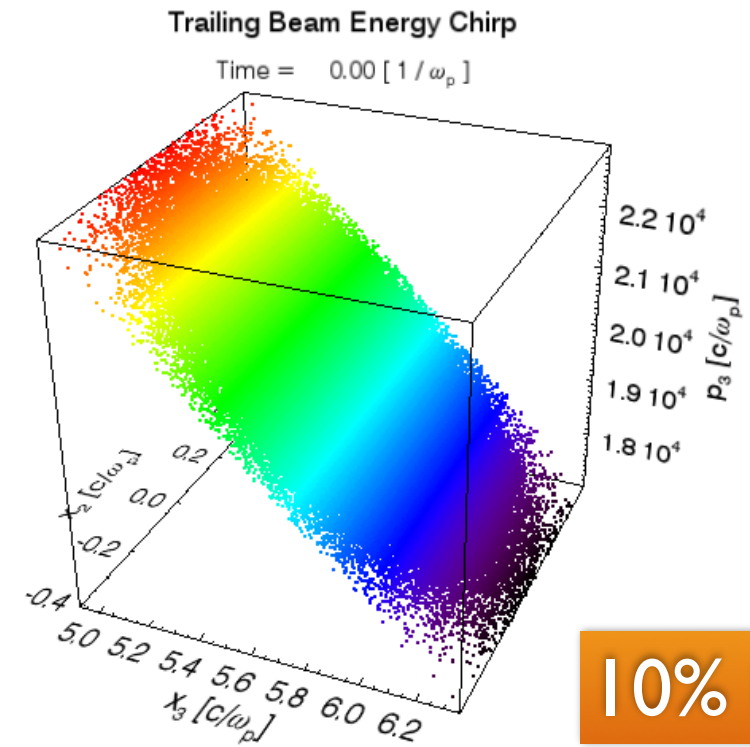
Center Slice

What about the trailing beam?

Drive Beam: $E = 10 \text{ GeV}$, $I_{\text{peak}} = 15 \text{ kA}$
 $\sigma_r = 3.65 \text{ }\mu\text{m}$, $\sigma_z = 12.77 \text{ }\mu\text{m}$,
 $N = 1.0 \times 10^{10}$ (1.6 nC), $\epsilon_N = 50 \text{ }\mu\text{m}$

Trailing Beam: $E = 10 \text{ GeV}$, $I_{\text{peak}} = 9 \text{ kA}$
 $\sigma_r = 3.65 \text{ }\mu\text{m}$, $\sigma_z = 6.38 \text{ }\mu\text{m}$,
 $N = 4.33 \times 10^9$ (0.69 nC), $\epsilon_N = 50 \text{ }\mu\text{m}$
 (transversely offset by 1 μm)

Distance between two bunches: 150 μm
Plasma Density: $4.0 \times 10^{16} \text{ cm}^{-3}$

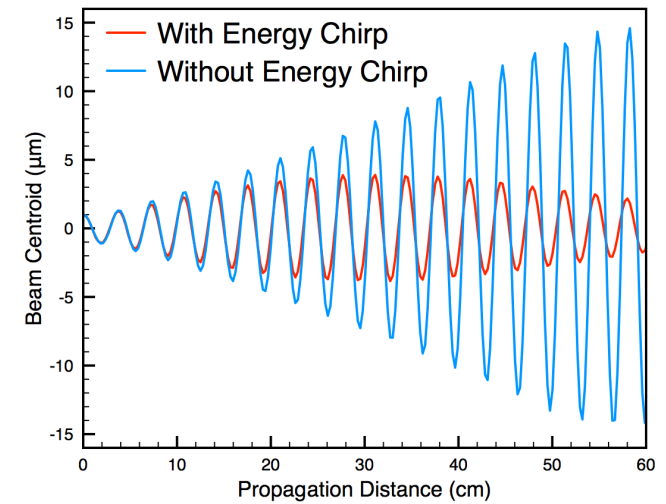
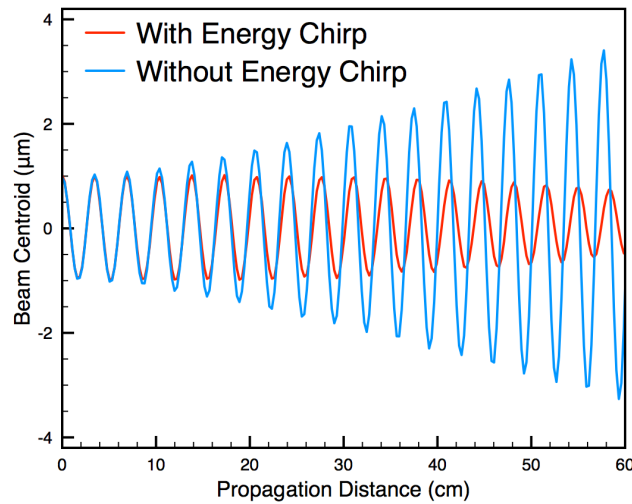
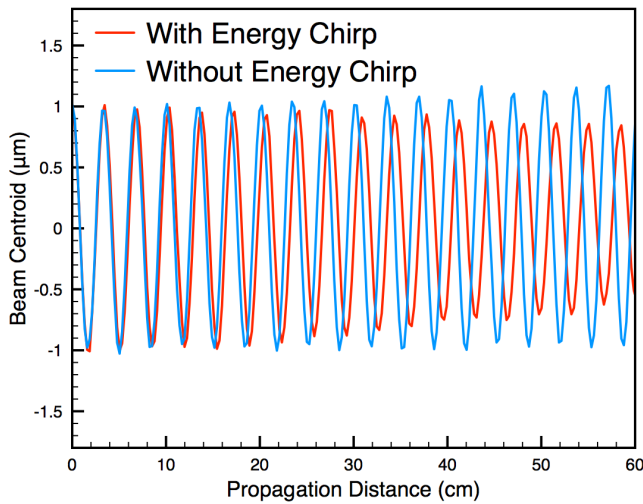


10% Energy Chirp

Head

Center

Tail



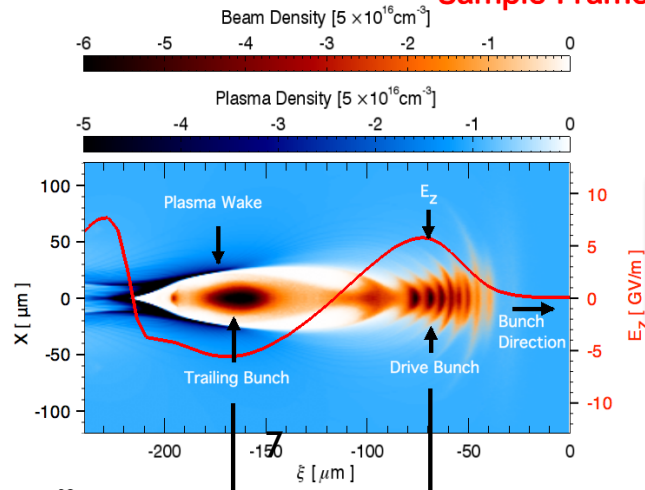
$$\xi = -\sigma_z$$

$$\xi = 0$$

$$\xi = \sigma_z$$

10% Energy Chirp

Propagation Distance \rightarrow S = 25.66 [cm] Sample Frame

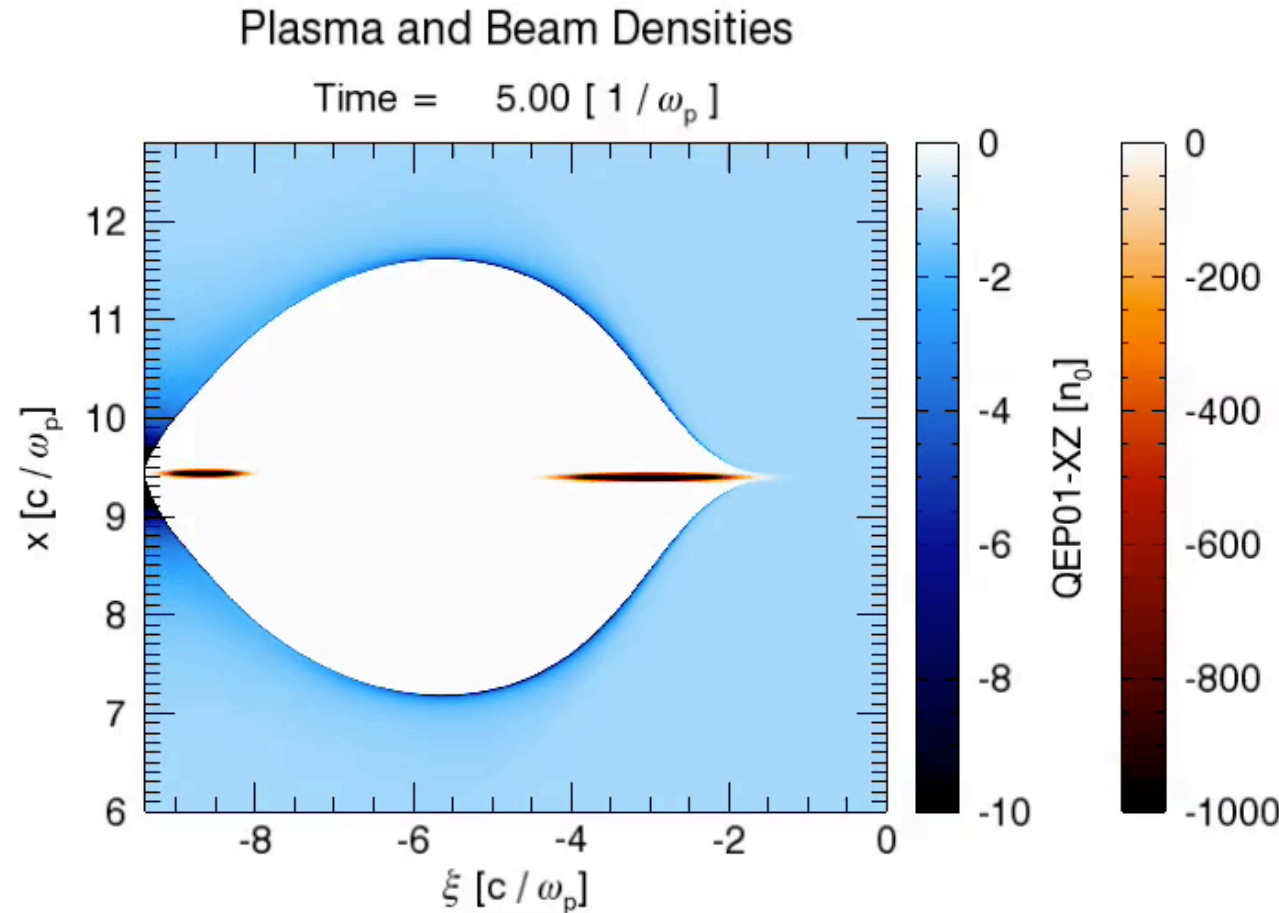


Overloading the Wake can compensate the chirp.

Drive Beam: $E = 10$ GeV, $I_{\text{peak}} = 15$ kA
 $\sigma_r = 0.516$ μm , $\sigma_z = 12.77$ μm ,
 $N = 1.0 \times 10^{10}$ (1.6 nC), $\epsilon_N = 1$ μmrad

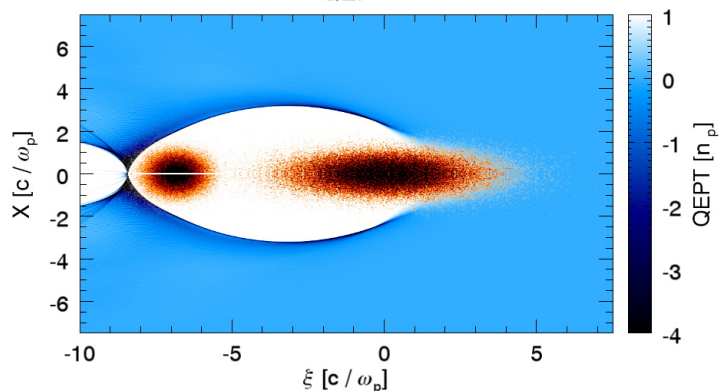
Trailing Beam: $E = 10$ GeV, $I_{\text{peak}} = 9$ kA
 $\sigma_r = 0.516$ μm , $\sigma_z = 6.38$ μm ,
 $N = 4.33 \times 10^9$ (0.69 nC), $\epsilon_N = 1$ μmrad
 (transversely offset by 1 μm)

Distance between two bunches:
 150 μm
Plasma Density:
 4.0×10^{16} cm^{-3} (Hydrogen)

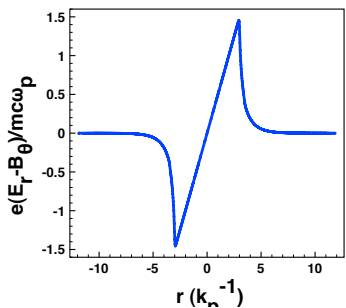
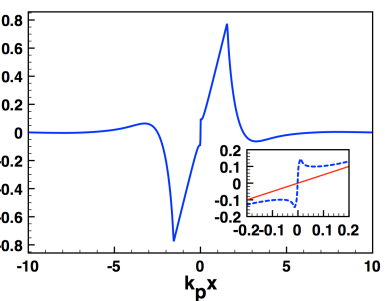
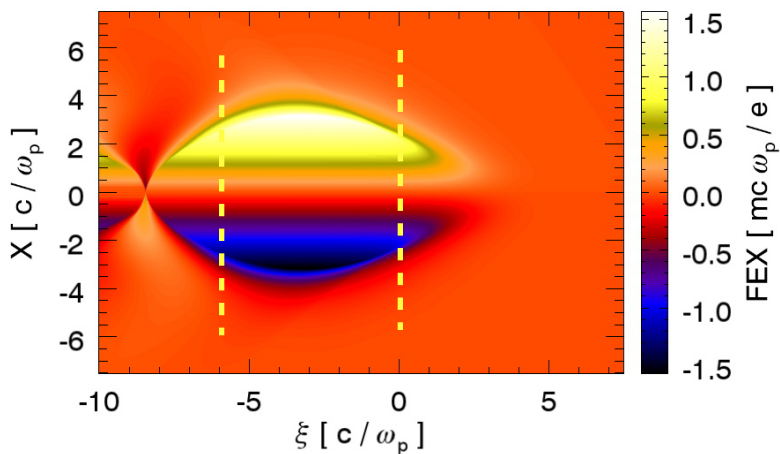


Blowout PWFA

QEP



Focusing Field ($E_r - B_\theta$)



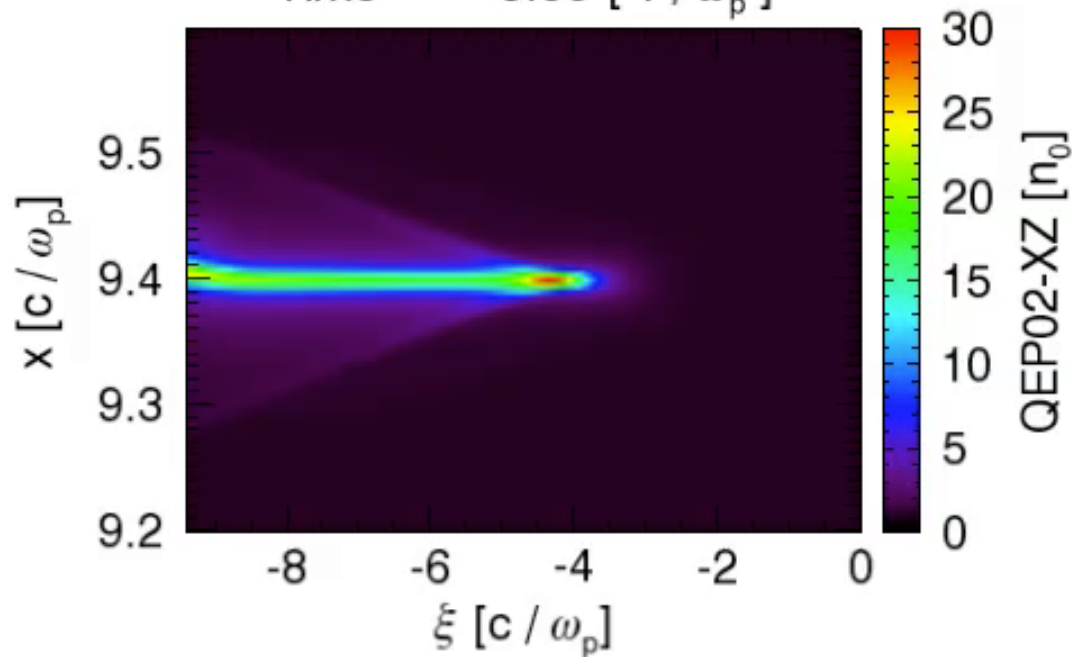
Plasma Ion Motion

(Talk on Thursday)

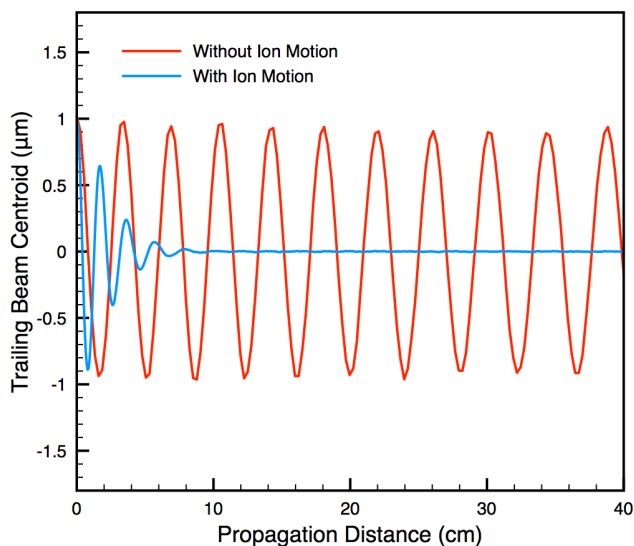


QEP02-XZ

Time = 5.00 [$1/\omega_p$]

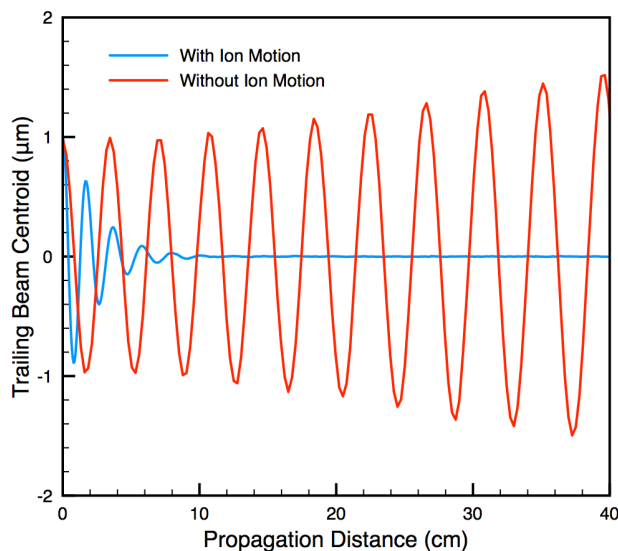


Head



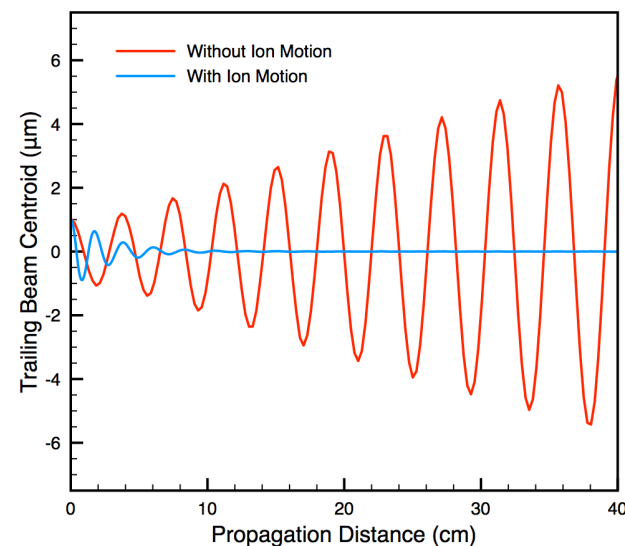
$$\xi = -\sigma_z$$

Center



$$\xi = 0$$

Tail



$$\xi = \sigma_z$$

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