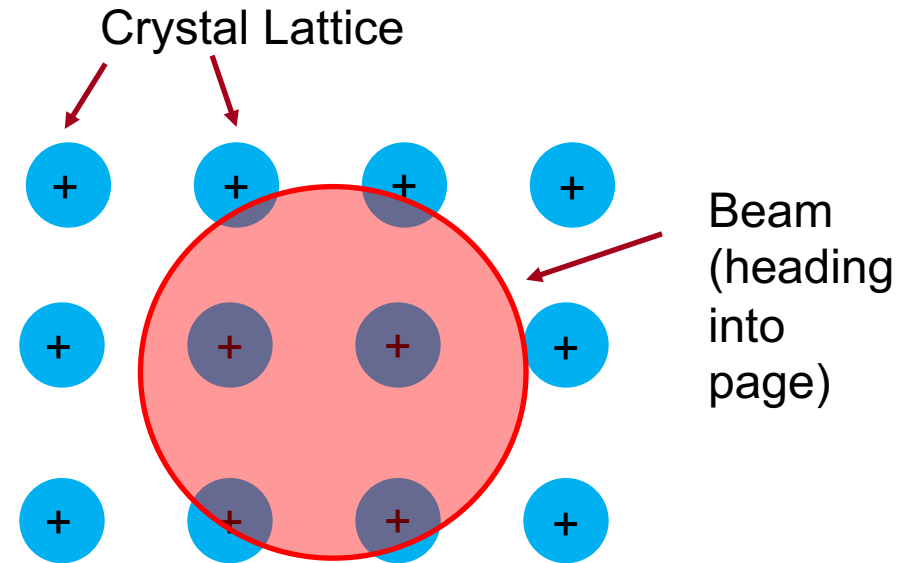


# Measuring Emittances with Crystals

Brendan O'Shea

# How does Crystal Channeling work?

- Each crystal is cut so that along the beam direction the atoms line up.
- Close enough to the atoms the potential is attractive for electrons.
- Electrons with sufficiently small transverse velocity are trapped in the potential.



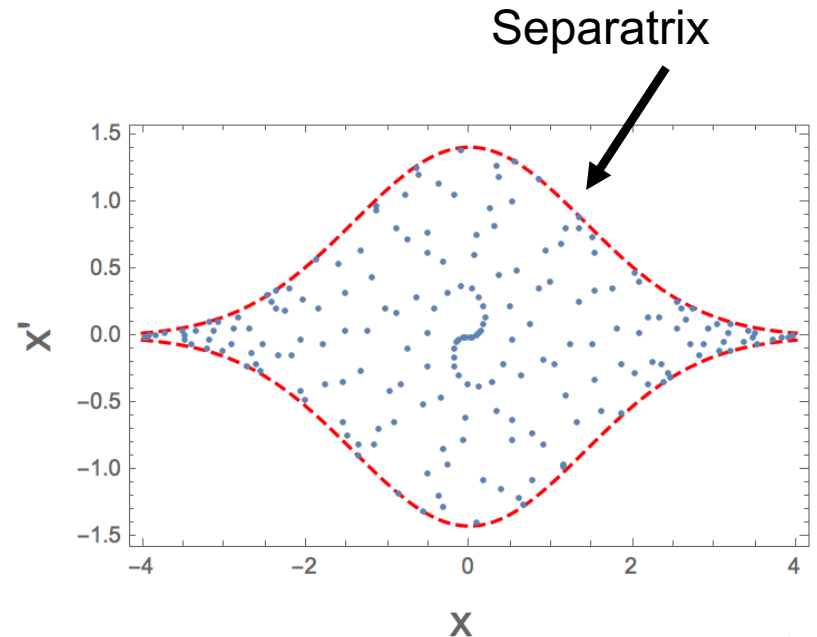
# Crystal Math

- Potential modeled as a Gaussian shape
- Critical angle  $\psi_c$  parameterizes acceptance of crystal channel
- Beta functions for each beam are assumed matched to the plasma,  $\lambda_p = 100 \mu\text{m}$

$$U(x) = U_0 \left(1 - e^{-\frac{x^2}{2a_0^2}}\right)$$

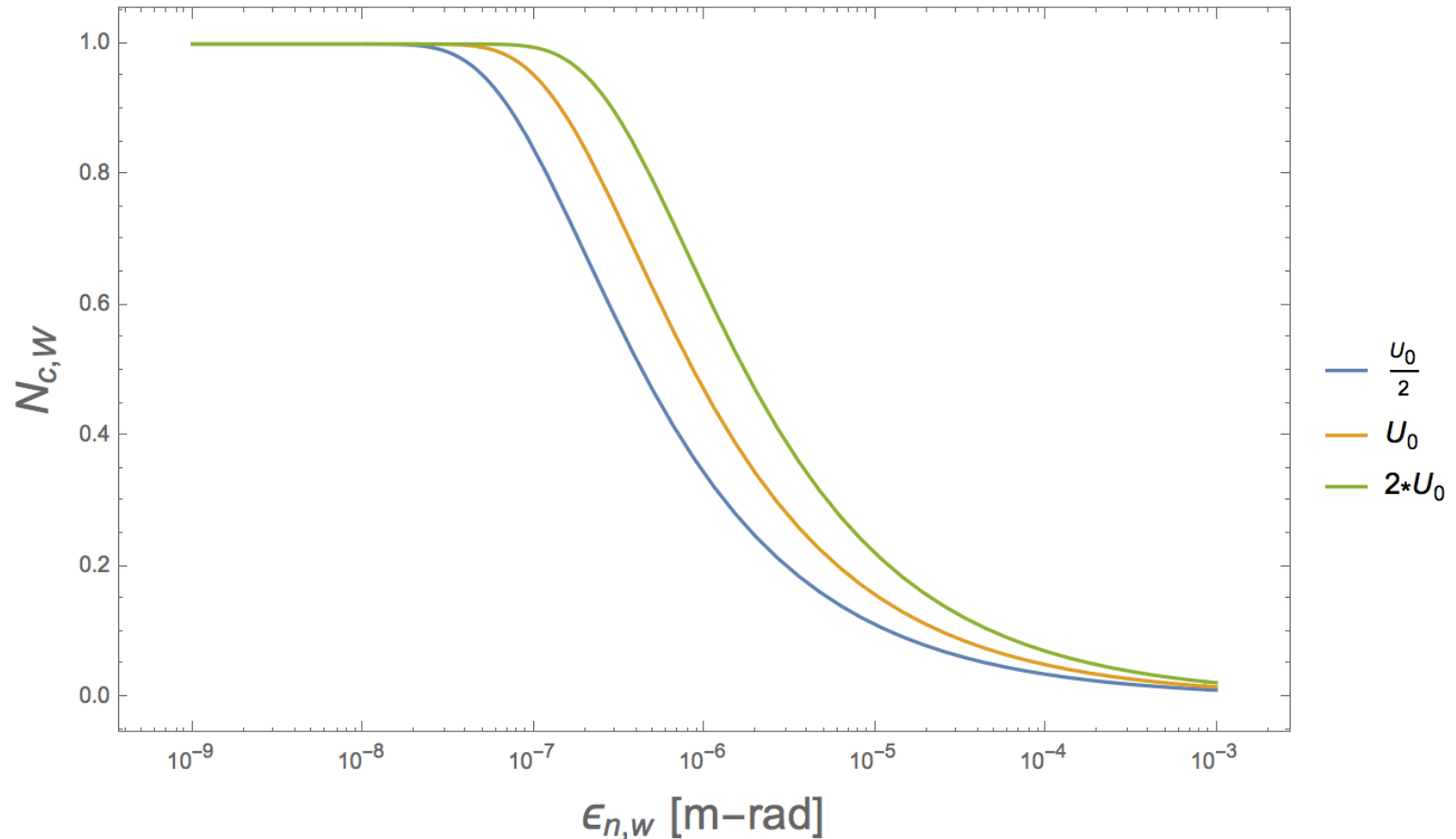
$$H_x = \frac{p^2 \psi^2}{2\gamma m} + U(x)$$

$$\psi_c^2 = \frac{2U_0}{\gamma m c^2}$$



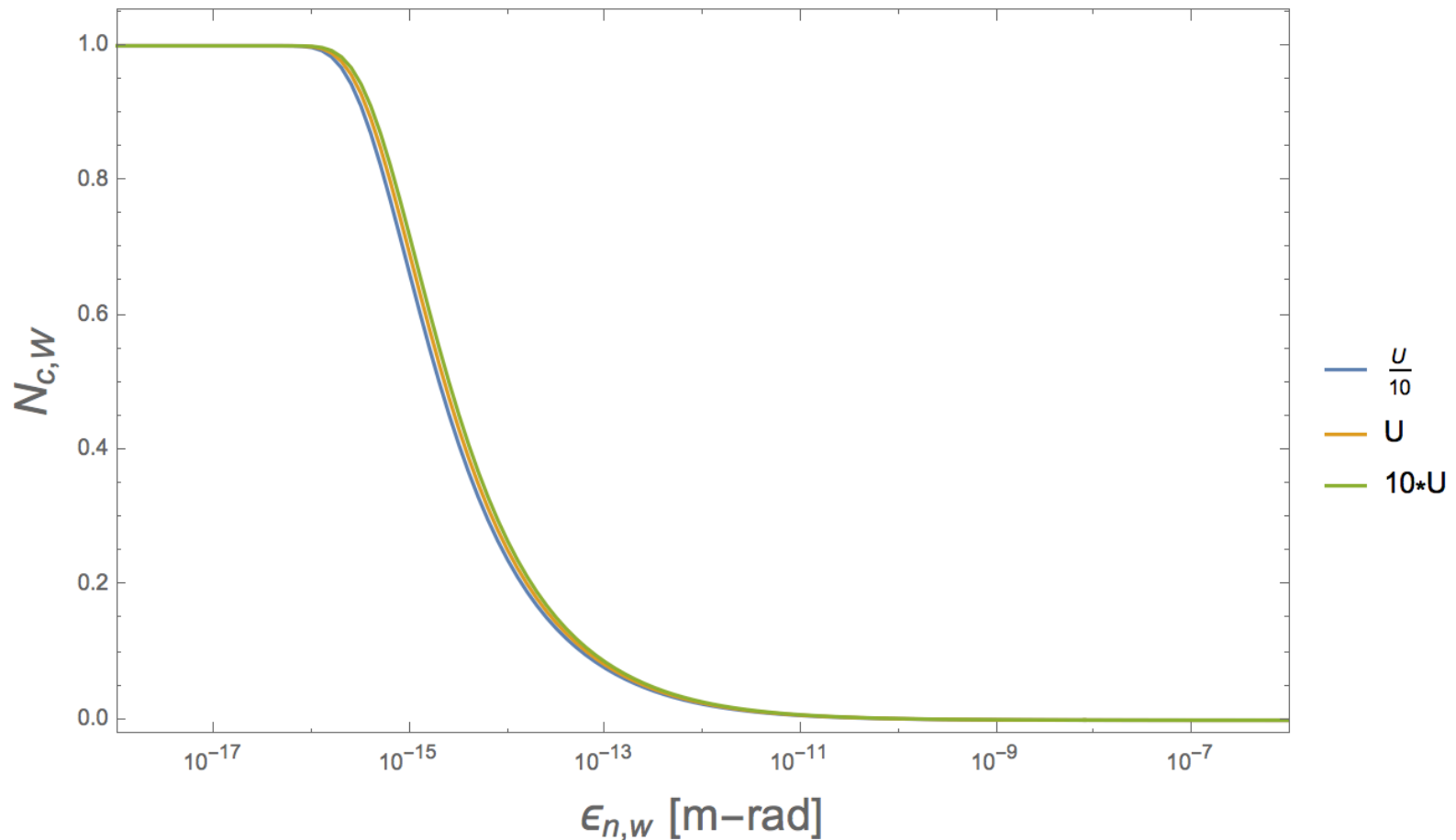
# Acceptance Ignoring the Spatial Dimension

$$N_c = \frac{1}{\sqrt{2\pi}\sigma_{x'}} \int_{-\psi_c}^{\psi_c} e^{-\frac{x'^2}{2\sigma_{x'}^2}} dx' = \text{Erf}\left[\frac{\psi_c}{\sqrt{2}\sigma_{x'}}\right]$$

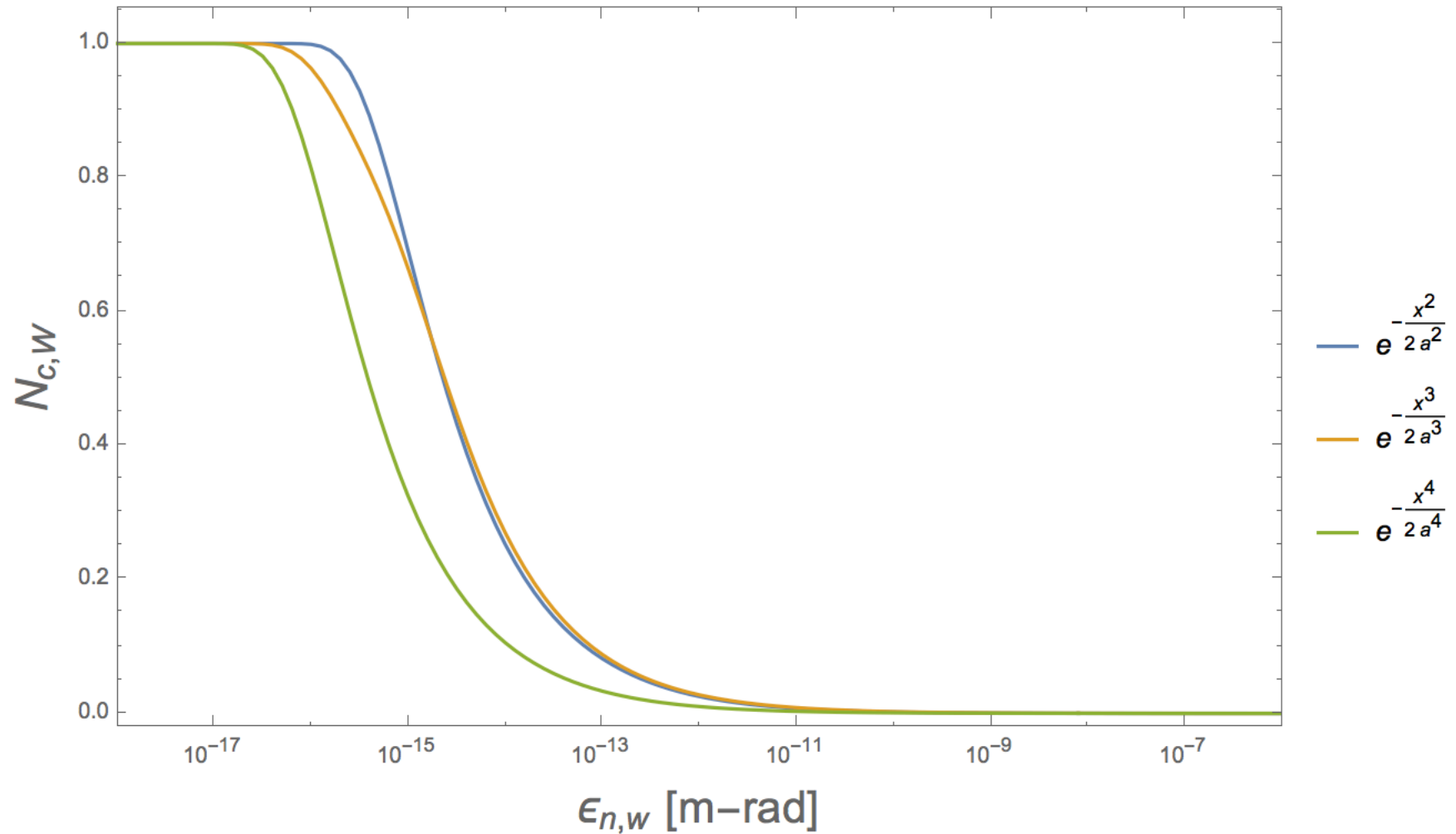


# A single potential well

$$N_c = \frac{1}{2\pi\sigma_{x'}\sigma_x} \int_{-\infty}^{\infty} dx \int_{-\psi_c e^{-\frac{x^2}{4a_0^2}}}^{\psi_c e^{-\frac{x^2}{4a_0^2}}} e^{-\frac{(x-x')^2}{2\sigma_x^2}} e^{-\frac{x'^2}{2\sigma_{x'}^2}} dx'$$



# A single potential well, part deux



# Challenges

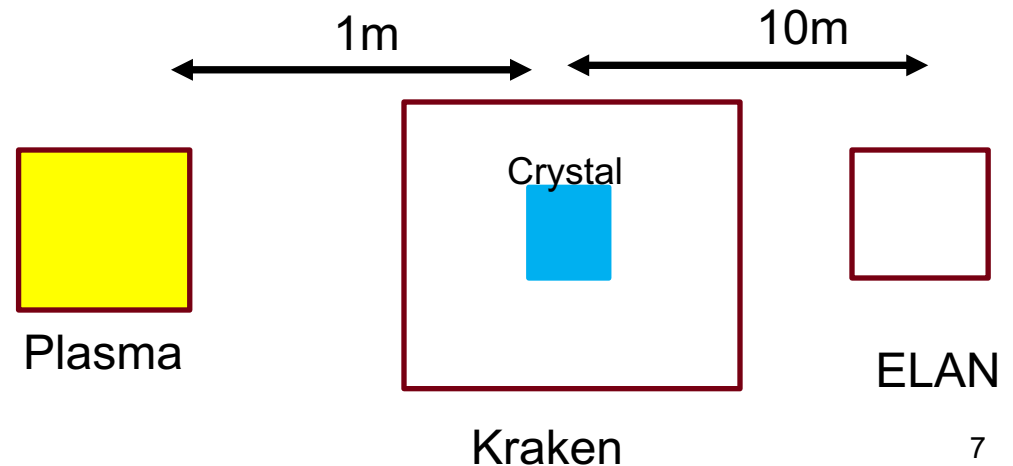
- Negative particles tend to hit the string, causing de-channeling
  - $L_d \sim 40 \mu\text{m}$
- Have to get angle correct for beam size:
  - Ex:  $\beta = 0.5\text{m}, \epsilon_n = 10^{-8}, \gamma = 2 \times 10^3$
  - $\sigma_x = 1\text{mm}$  @ELAN
  - Crystal bend of  $300 \mu\text{rad} \rightarrow 3\text{mm}$
- Crystal Length  $\sim 40 \mu\text{m}$

$$n = n_0 e^{-\frac{z}{L_d}}$$



Relative intensities:  $\bullet \geq 2, / \geq 3, \backslash \geq 4, \times \geq 5, \nabla \geq 6, \blacksquare \geq 7$

Fig. 7. 15 GeV/c  $\pi^-$  incident on a 4.2 mm Ge single crystal. Same plot and condition as in fig. 6. Here planar effects are absent but there is a peak in the axial direction surrounded by a low-intensity region. Note that the axial peak is lower than the random "plateau" far from the axis. There are 10 000 events in the plot.



- To Understand:
- Shape of the potential
- Beam transfer from plasma to vacuum and distance from plasma to crystal
- Effect of beam on crystal
  - string re-ordering due to temperature
  - string damage
- A better understanding of electron-string collisions